

How to measure dose?

- Demystifying TG21

Presenter: Chengzhu Zhang

Residency 2023~2024

Rotation Mentor: Xiao Wang

09/12/2023

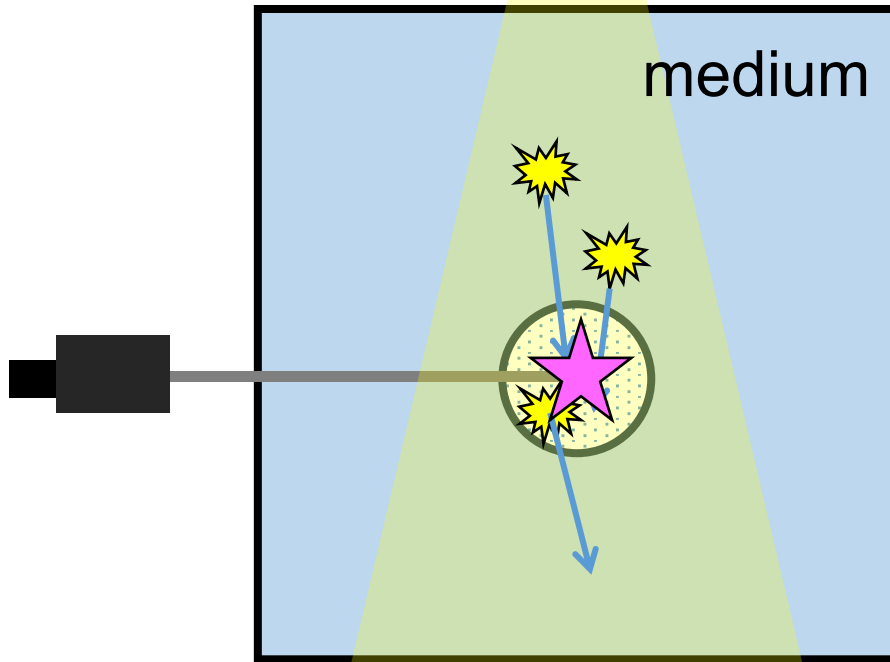
RUTGERS

Robert Wood Johnson
Medical School

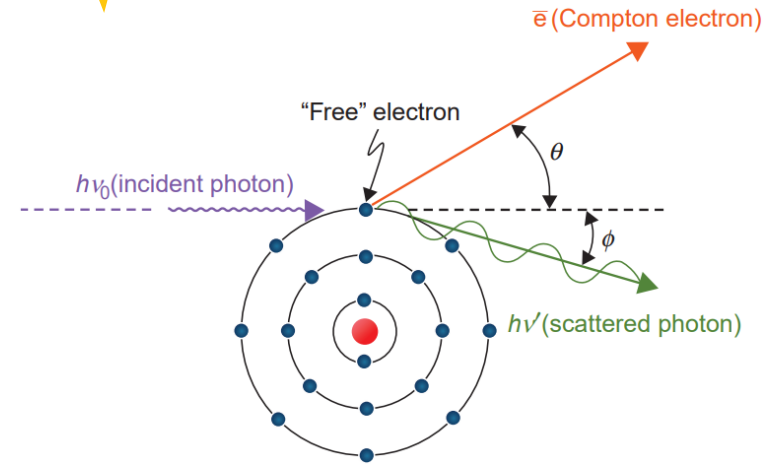
- TG-51
 - Reading to dose: Calibration factor $N_{d,w}$
 - Standard to user beam: Beam quality factor k_Q
- TG-21



Difficulties measuring the dose



★ Compton Scattering $\propto \rho_e$

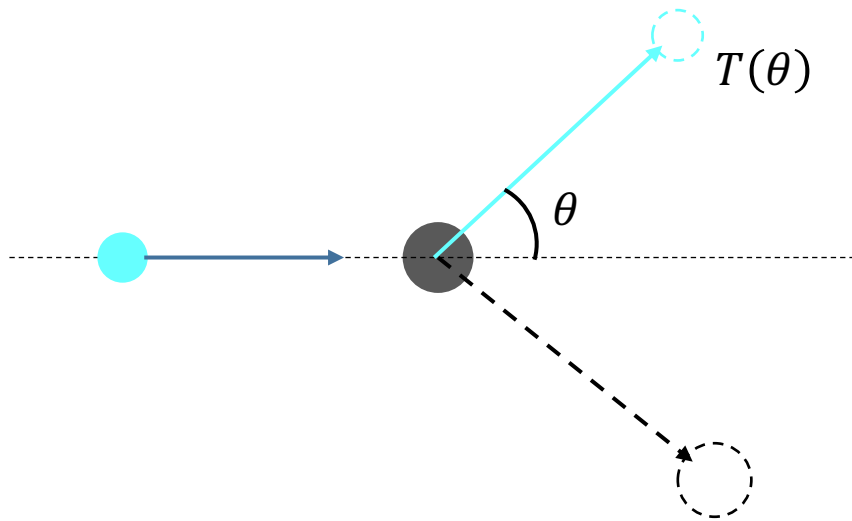


Dose is not directly measurable ...

- Compton Scattering
- Rayleigh Scattering
- Photoelectric interaction
- Pair/Triplet Production

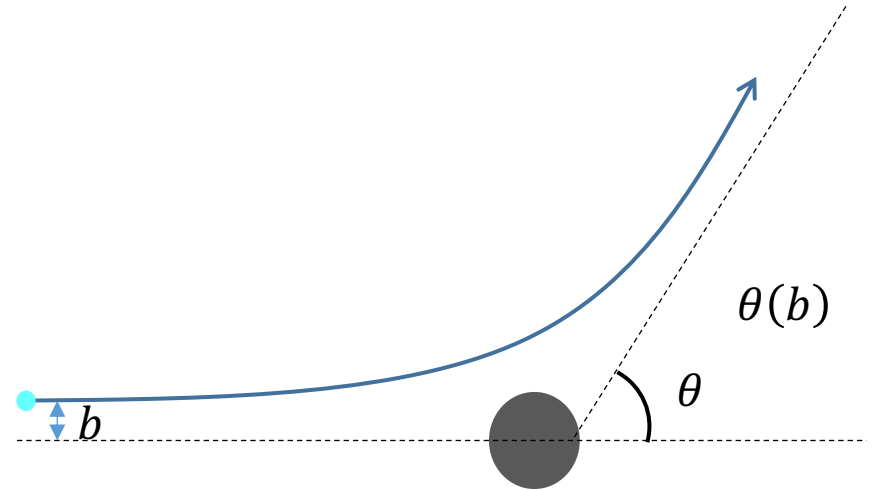
The physical picture of stopping power

Two-body Collision



Angular Energy Transfer
(Energy)

Coulomb Scattering



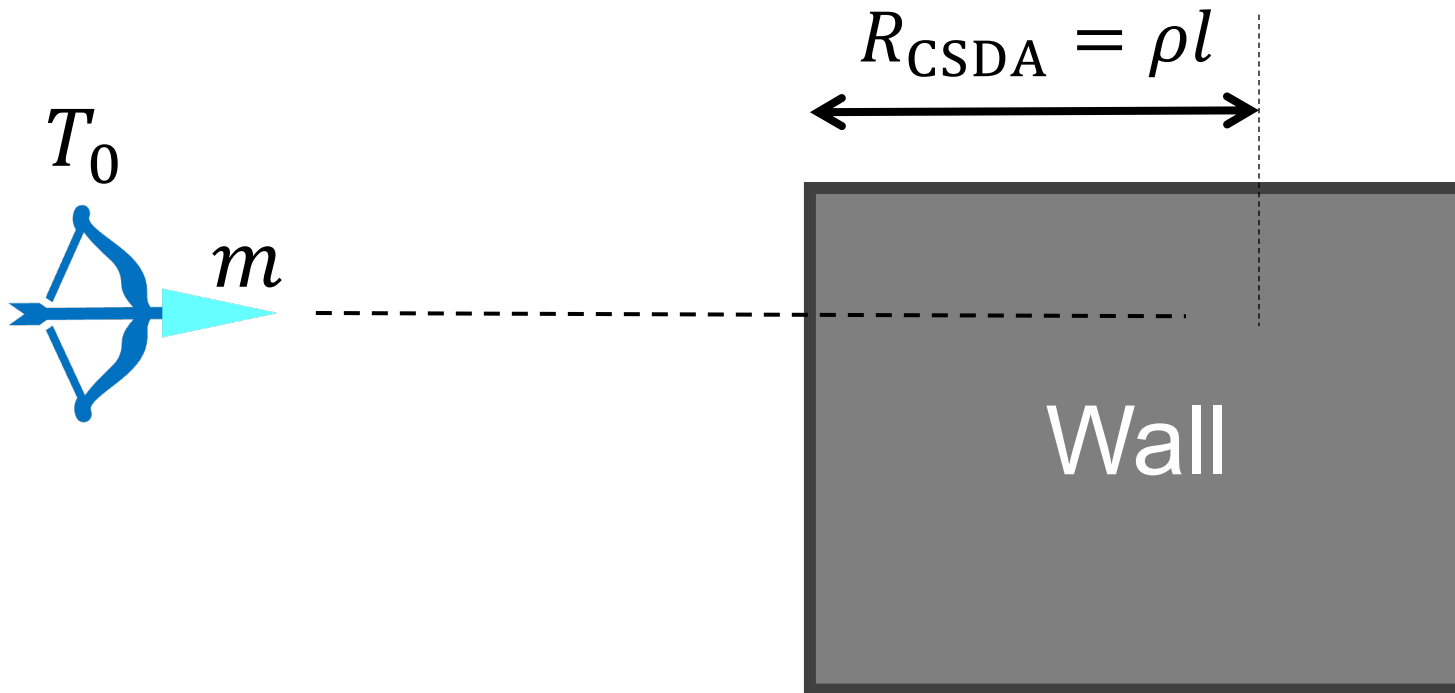
Angular Cross Section
(Probability)

Total Energy Transferred

$$E_{\text{tr}} = \int T(\theta) db(\theta)$$

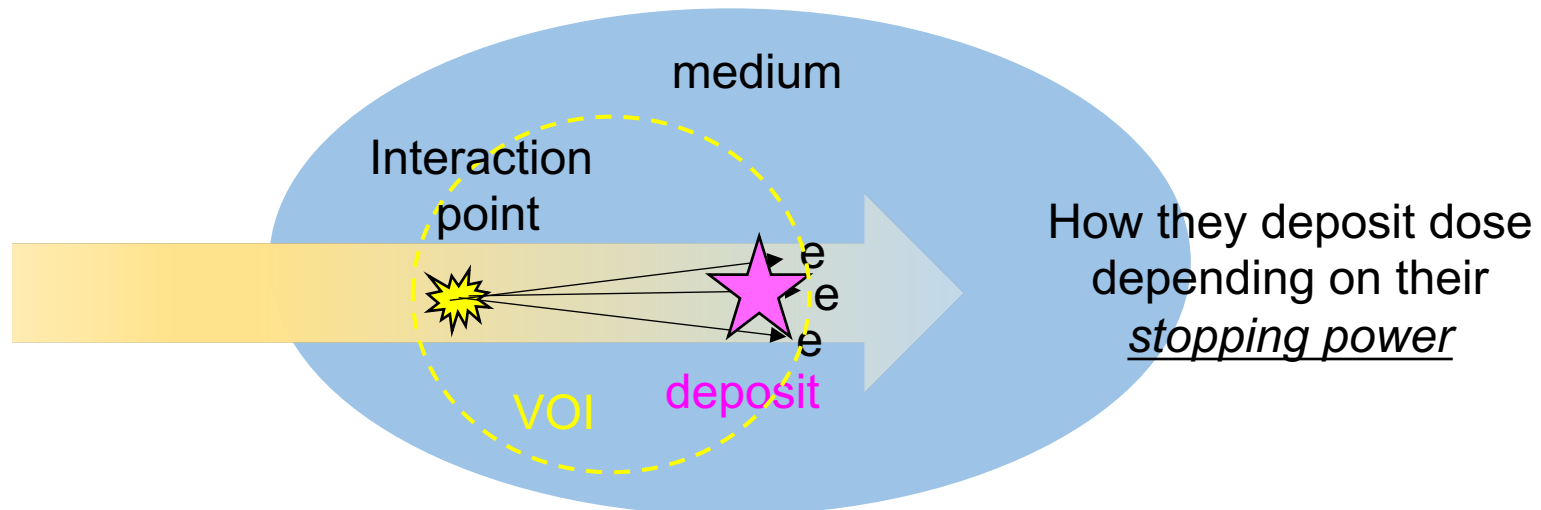
What is stopping power?

- For charged particle interaction



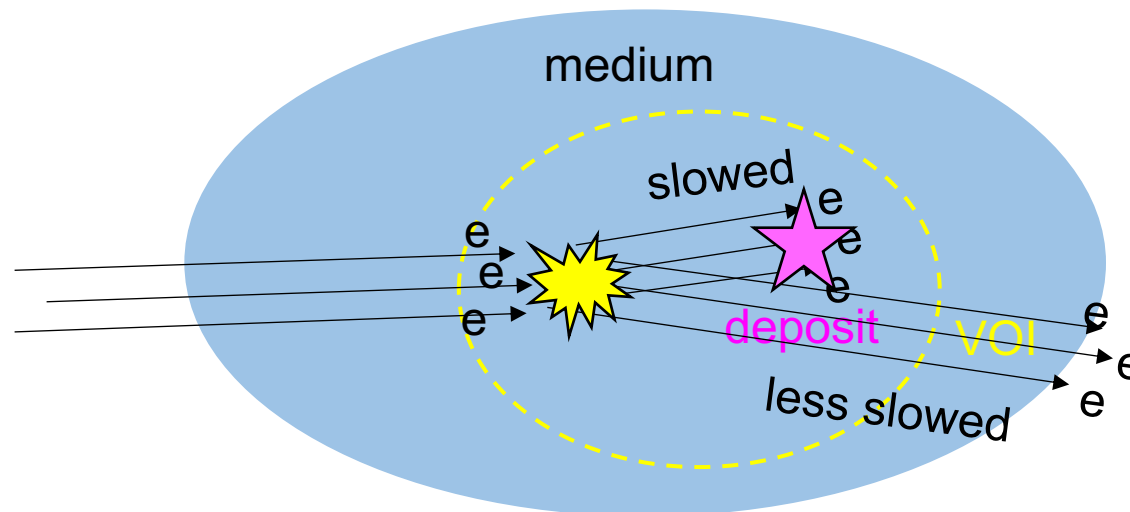
How photon beam deposits dose? **RUTGERS**

- From photon perspective:
 - The photon fluence attenuates.
 - Photon energies are transferred to electrons.
 - The secondary electrons deposit energy → dose.
 - Secondary electron spectrum remain similar.

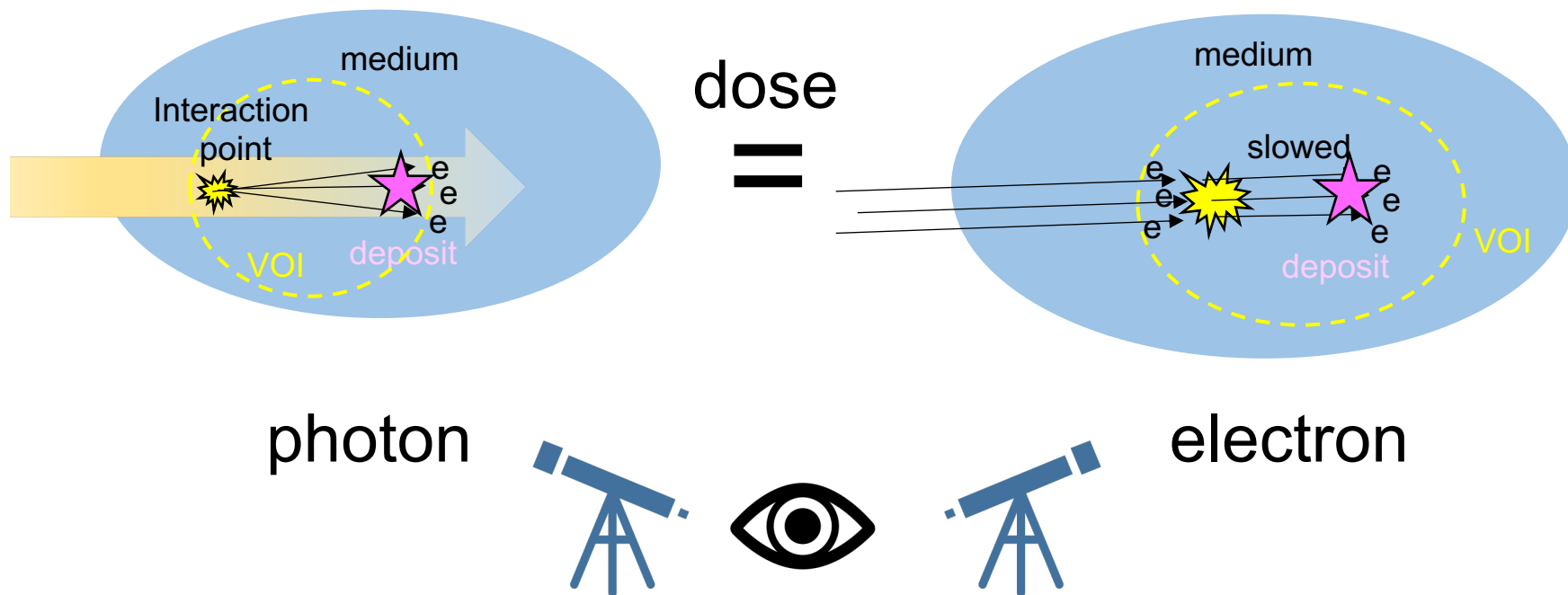


How electron beam deposits dose?

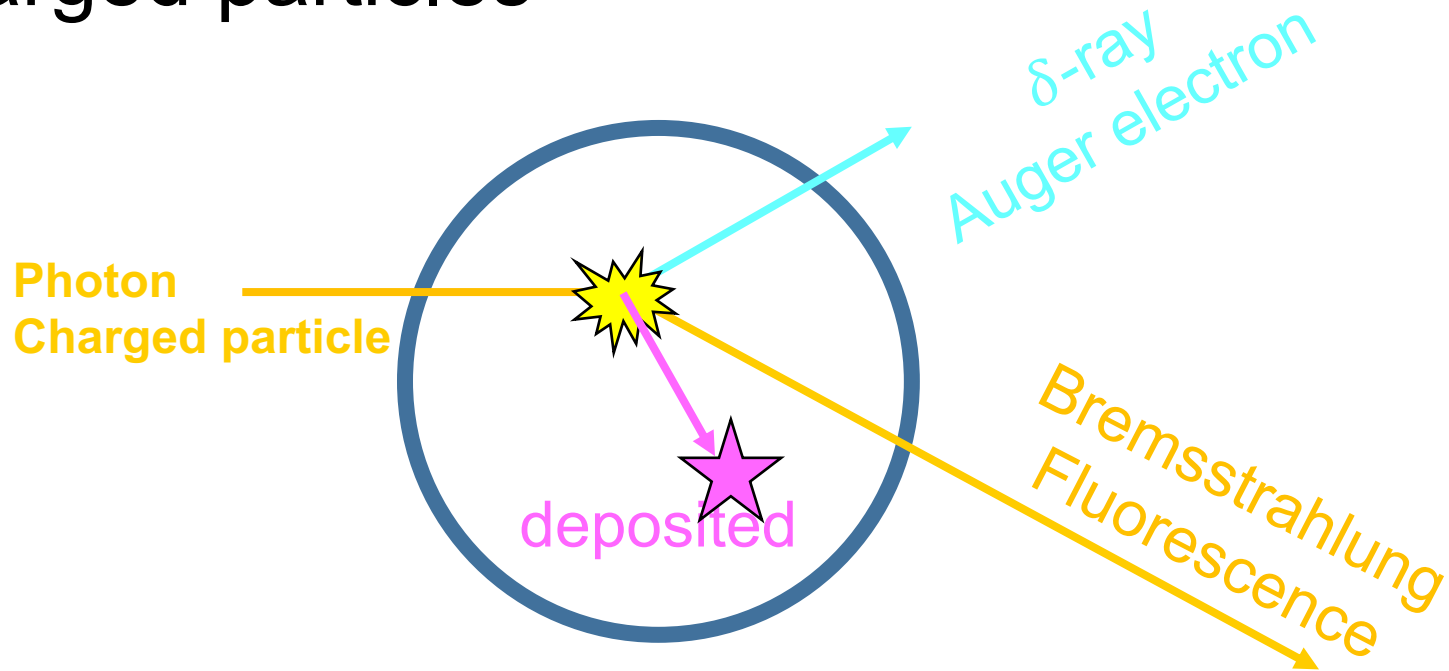
- From electron perspective
 - Electrons continuously slow down ($E \downarrow$)
 - Secondary electrons spectrum varies with depth.
 - Considering energy transfer lower than a threshold (Δ) \rightarrow “restricted”
 - Energy deposit locally.



☆ Dose equivalency

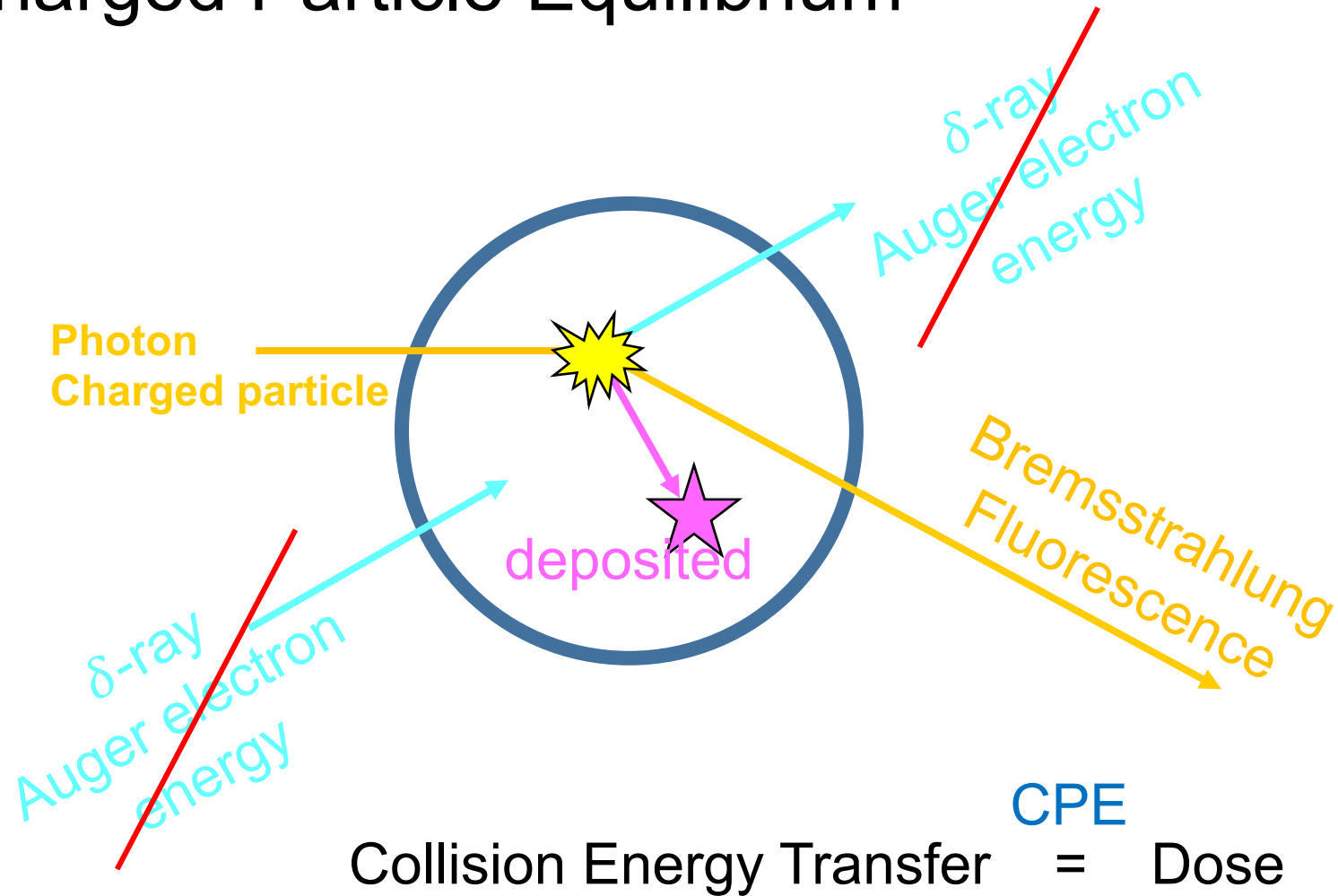


- Energy Transfer among radiation and charged particles

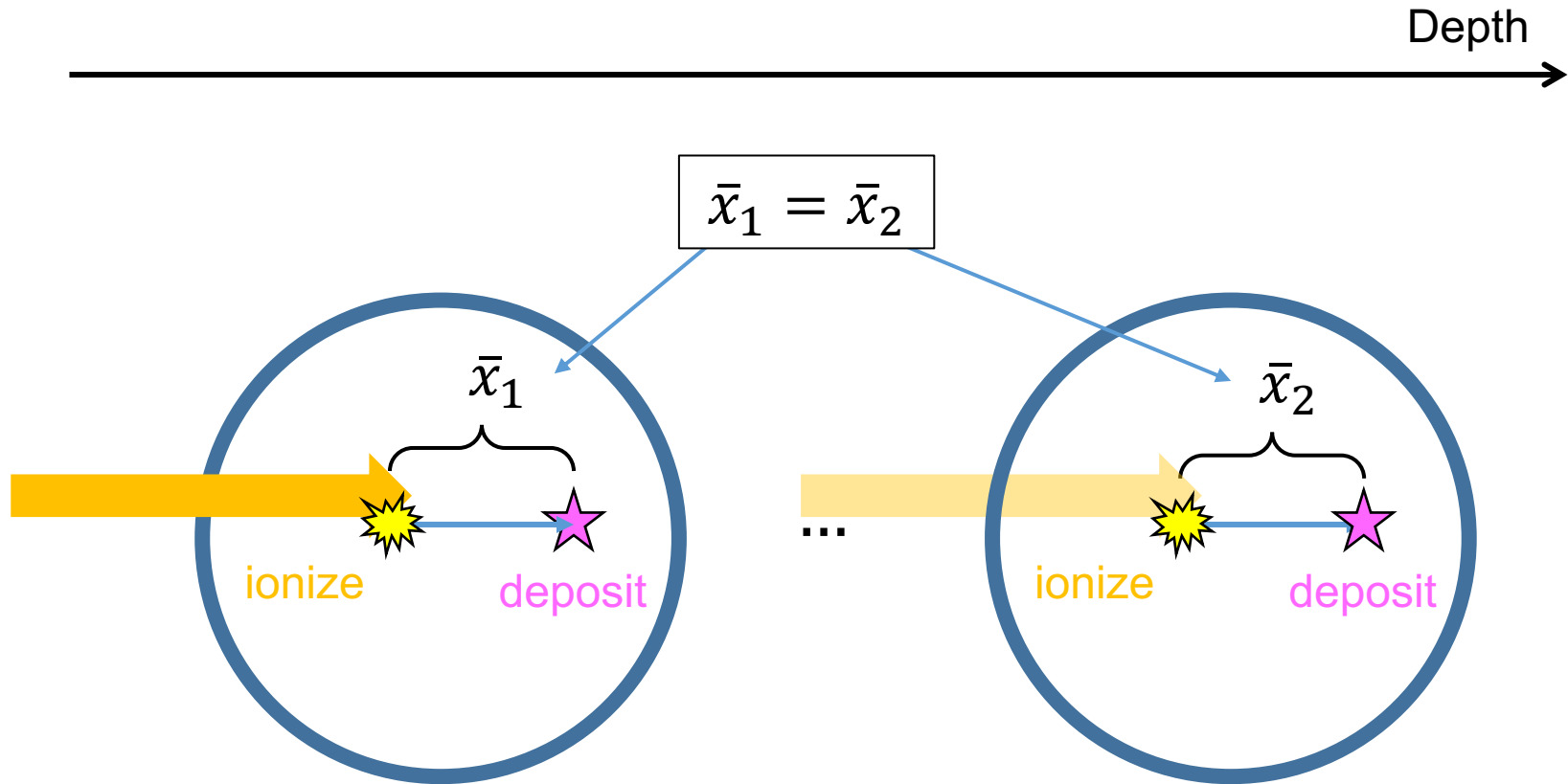


Energy transfer (K) \neq Dose

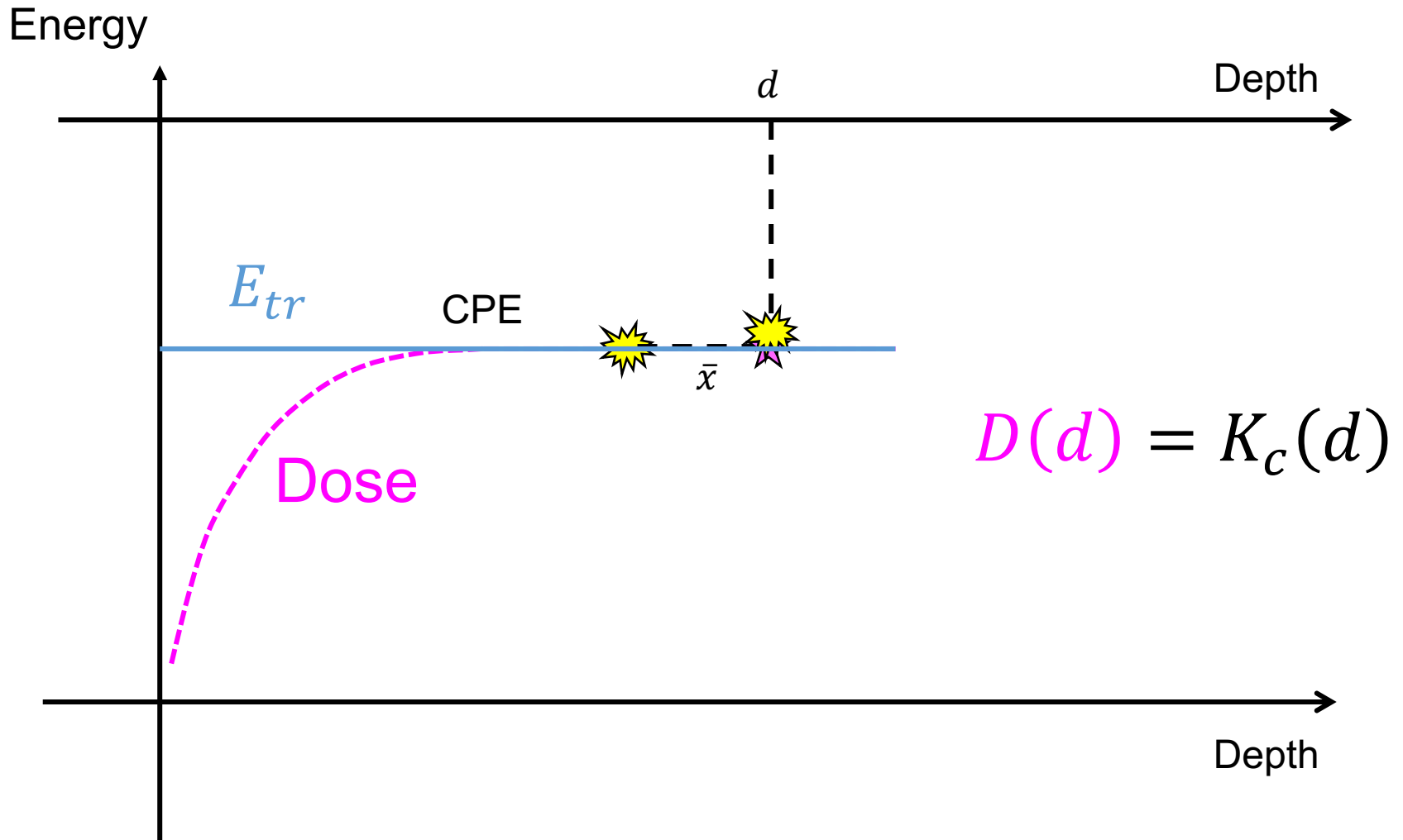
■ Charged Particle Equilibrium



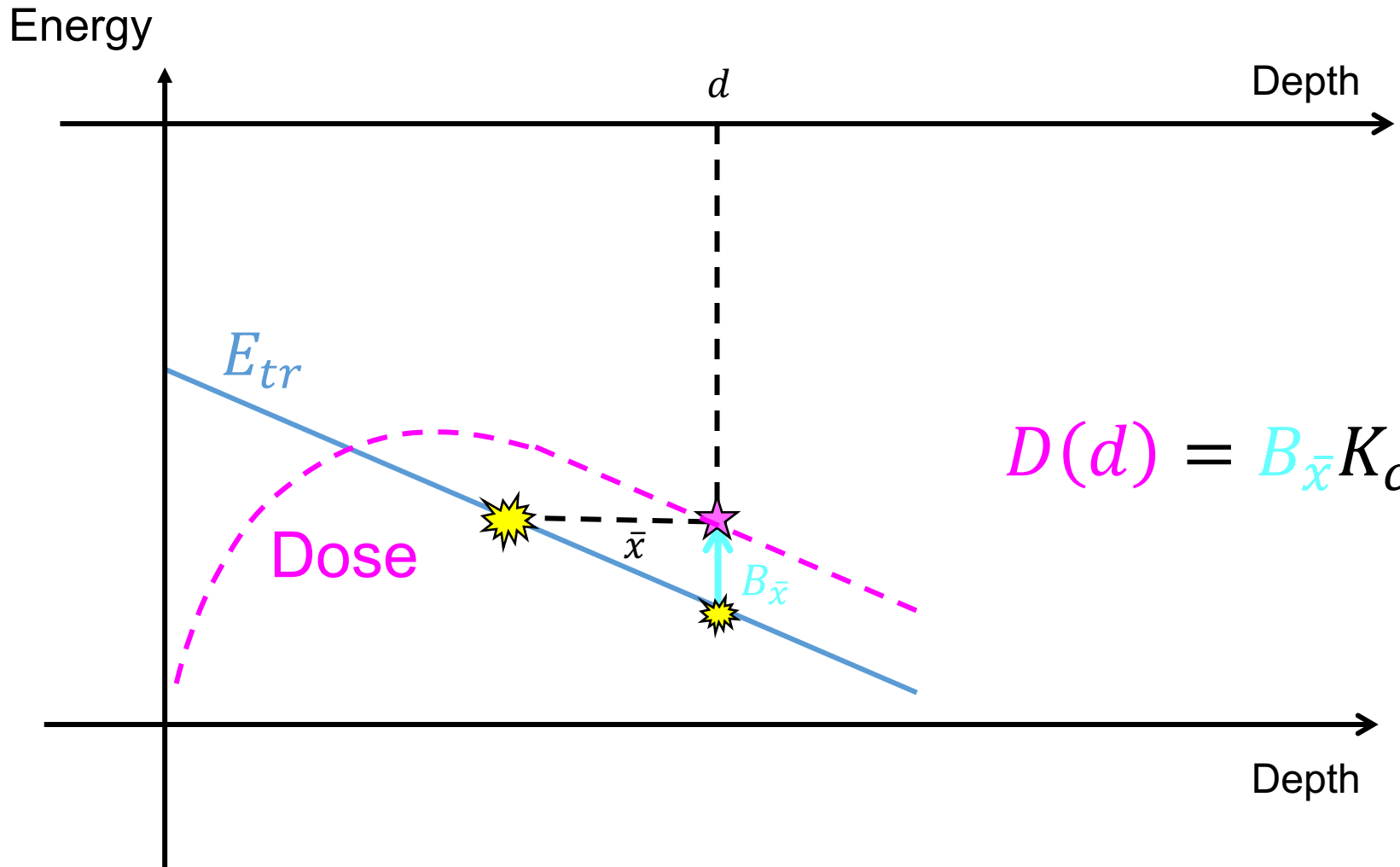
Transient CPE



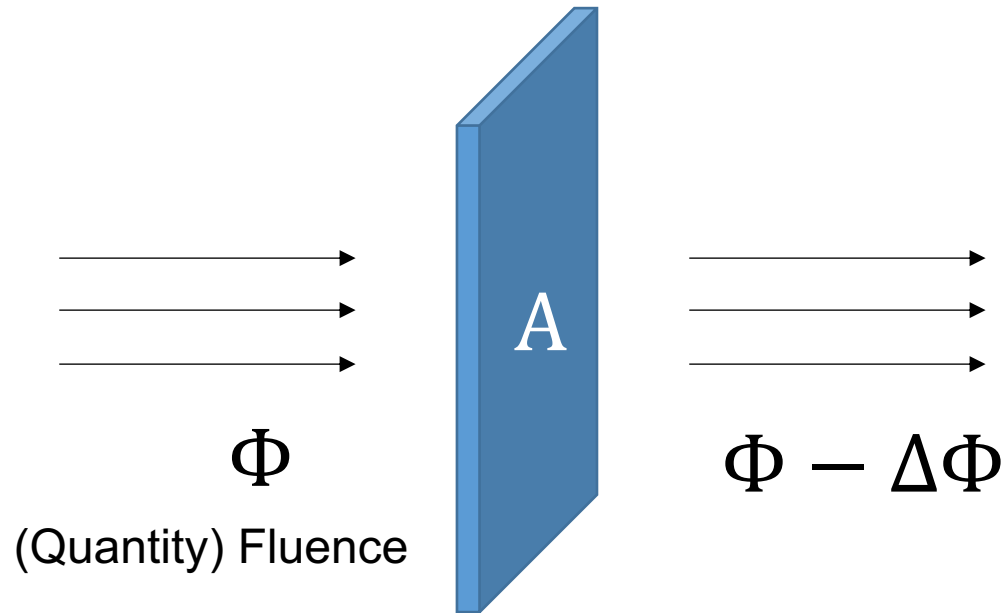
same photon-energy \rightarrow same secondary electron spectrum



TCPE curve

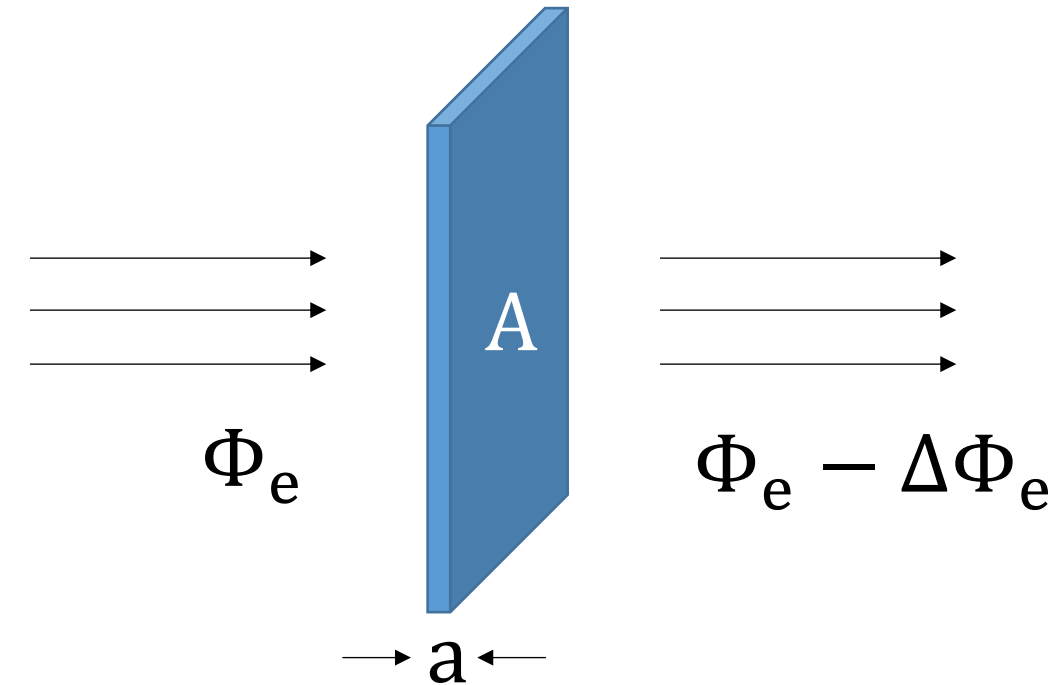


$$D(d) = B_{\bar{x}} K_c(d)$$



$\rightarrow a \leftarrow$
 K_c
 TCPE
 $D \leftarrow$
 KERMA = $\frac{E_{tr}^c}{m}$
 $= E\Phi(E) \left(\frac{\mu_{ab}(E)}{\rho} \right)$

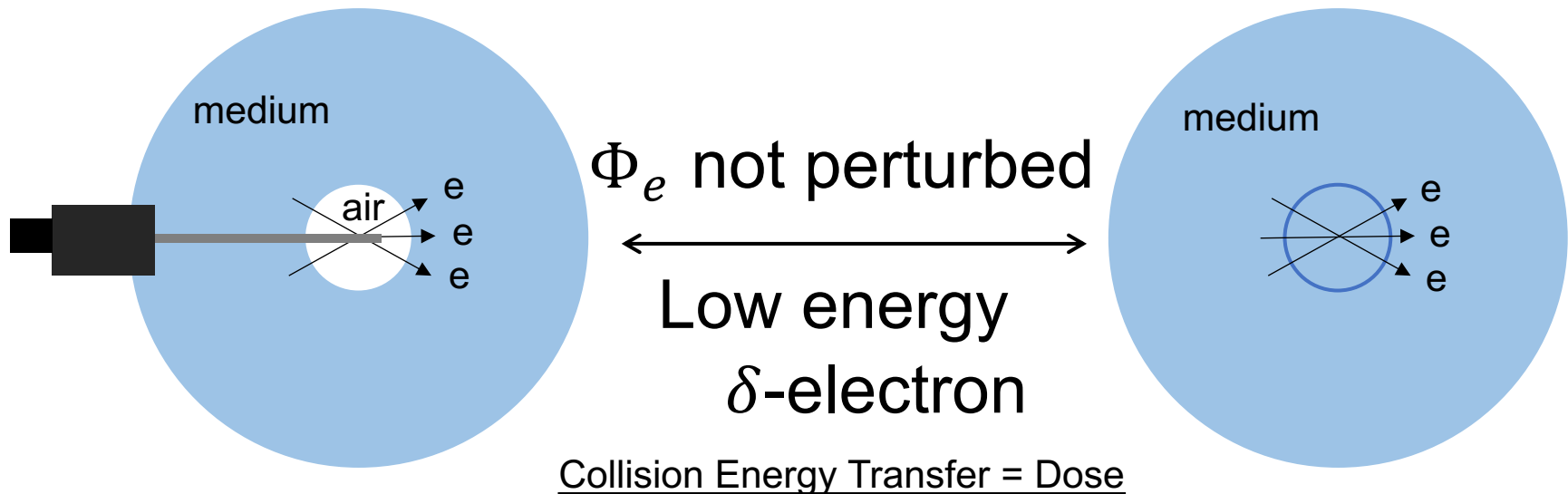
Energy Fluence



$$\begin{aligned}
 \boxed{D}^{\text{local}} & \leftarrow \text{CEMA} = \frac{E_{tr}^c}{m} \\
 & = \Phi_e(E) \left(\frac{S_{col}(E)}{\rho} \right)
 \end{aligned}$$

Quantity Fluence

Bragg-Gray Cavity Theory (Small Cavity)



$$D_{\text{air}}(E) \longrightarrow D_{\text{med}}(E)$$
$$= \Phi_e(E) \left(\frac{S}{\rho} \right)_{\text{air}}(E) \qquad = \Phi_e(E) \left(\frac{S}{\rho} \right)_{\text{med}}(E)$$

Bragg-Gray Cavity Theory (Small Cavity)

$$D_{\text{air}} = \int dE \Phi_e(E) \left(\frac{S}{\rho}\right)_{\text{air}}(E) \quad D_{\text{med}} = \int dE \Phi_e(E) \left(\frac{S}{\rho}\right)_{\text{med}}(E)$$

$$\frac{D_{\text{med}}}{D_{\text{air}}} = \frac{\int dE \Phi_e(E) \left(\frac{S}{\rho}\right)_{\text{med}}(E)}{\int dE \Phi_e(E) \left(\frac{S}{\rho}\right)_{\text{air}}(E)}$$

Bragg-Gray Cavity Theory (Small Cavity)

$$D_{\text{air}} = \int dE \Phi_e(E) \left(\frac{S}{\rho}\right)_{\text{air}}(E) \quad D_{\text{med}} = \int dE \Phi_e(E) \left(\frac{S}{\rho}\right)_{\text{med}}(E)$$

$$\frac{D_{\text{med}}}{D_{\text{air}}} = \frac{\frac{\int dE \Phi_e(E) \left(\frac{S}{\rho}\right)_{\text{med}}(E)}{\int dE \Phi_e(E)}}{\frac{\int dE \Phi_e(E) \left(\frac{S}{\rho}\right)_{\text{air}}(E)}{\int dE \Phi_e(E)}}$$

Normalized by $\Phi_e(E)$

Bragg-Gray Cavity Theory (Small Cavity)

$$D_{\text{air}} = \int dE \Phi_e(E) \left(\frac{S}{\rho}\right)_{\text{air}}(E) \quad D_{\text{med}} = \int dE \Phi_e(E) \left(\frac{S}{\rho}\right)_{\text{med}}(E)$$

bar means
"average" effect

$$\frac{D_{\text{med}}}{D_{\text{air}}} = \frac{\left(\overline{\frac{S}{\rho}}\right)_{\text{med}}}{\left(\overline{\frac{S}{\rho}}\right)_{\text{air}}}$$

Normalized by $\Phi_e(E)$

Bragg-Gray Cavity Theory (Small Cavity)

$$D_{\text{air}} = \int dE \Phi_e(E) \left(\frac{S}{\rho} \right)_{\text{air}}(E) \quad D_{\text{med}} = \int dE \Phi_e(E) \left(\frac{S}{\rho} \right)_{\text{med}}(E)$$

$$\frac{D_{\text{med}}}{D_{\text{air}}} = \left(\frac{\overline{S}}{\rho} \right)_{\text{air}}^{\text{med}}$$

Normalized by $\Phi_e(E)$

Bragg-Gray Cavity Theory (Small Cavity)

$$\frac{BK_{\text{med}}}{BK_{\text{air}}} \xleftarrow{\text{TCPE}} \frac{K_{\text{med}}}{K_{\text{air}}} = \left(\frac{\bar{\mu}}{\rho} \right)_{\text{air}}^{\text{med}}$$

Normalized by $\Psi(E)$

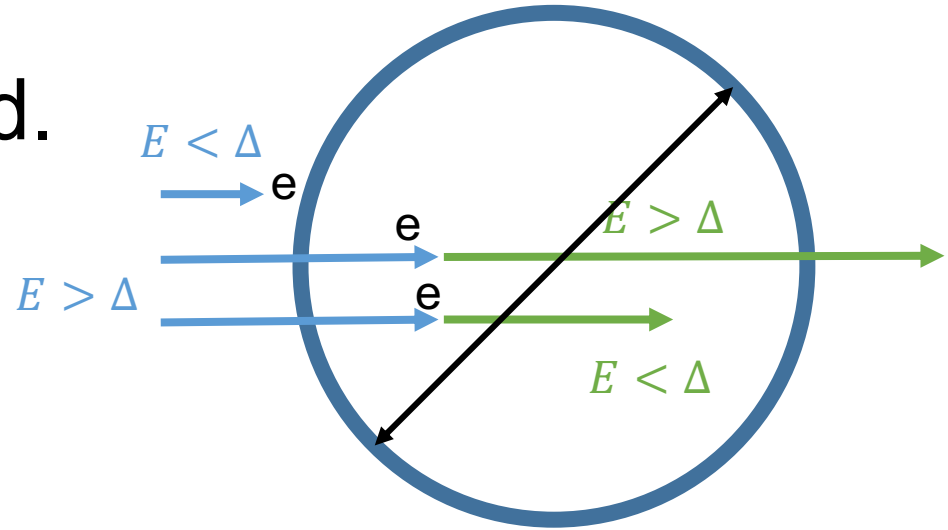
same build-up $B_{\bar{x}}$

Bragg-Gray Cavity Theory (Small Cavity)

$$\frac{D_{\text{med}}}{D_{\text{air}}} \xleftarrow{\text{TCPE}} \frac{K_{\text{med}}}{K_{\text{air}}} = \left(\frac{\bar{\mu}}{\rho} \right)_{\text{air}}^{\text{med}}$$

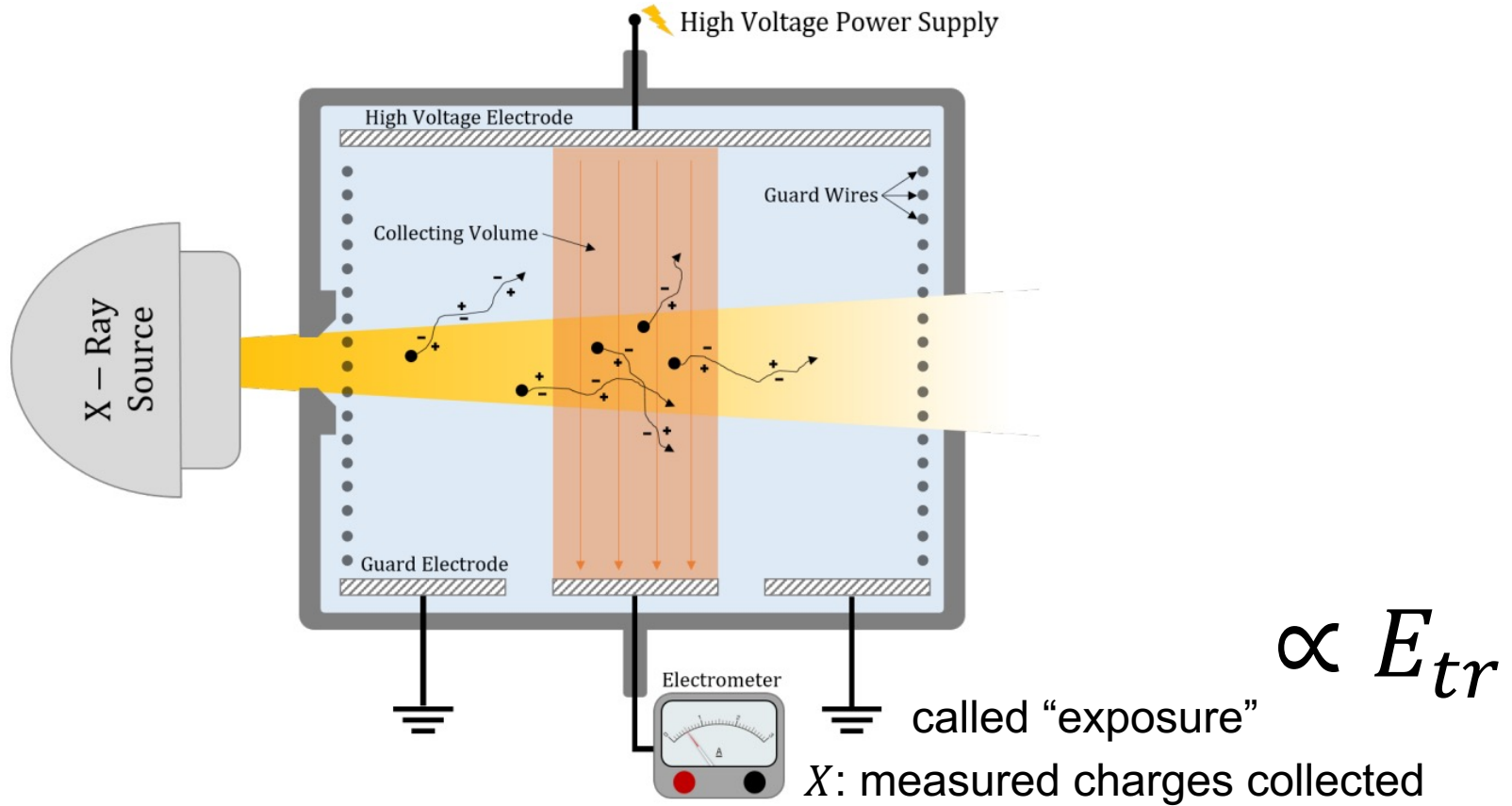
Normalized by $\Psi(E)$

- Δ : chamber size related.
- Only electron energy $> \Delta$ can enter the cavity.
- Only of energy $< \Delta$ deposits energy in the volume, becoming “dose”.



$$D_{\text{cavity}} = \int_{\Delta}^{E_{\text{max}}} dE \Phi(E) \left(\frac{S}{\rho} \right)_{\Delta} (E)$$

Measuring dose in free air



$$K_{c \text{ air}} = \left(\frac{X}{e} \right) \bar{W} = X \left(\frac{\bar{W}}{e} \right)_{\text{air}}$$

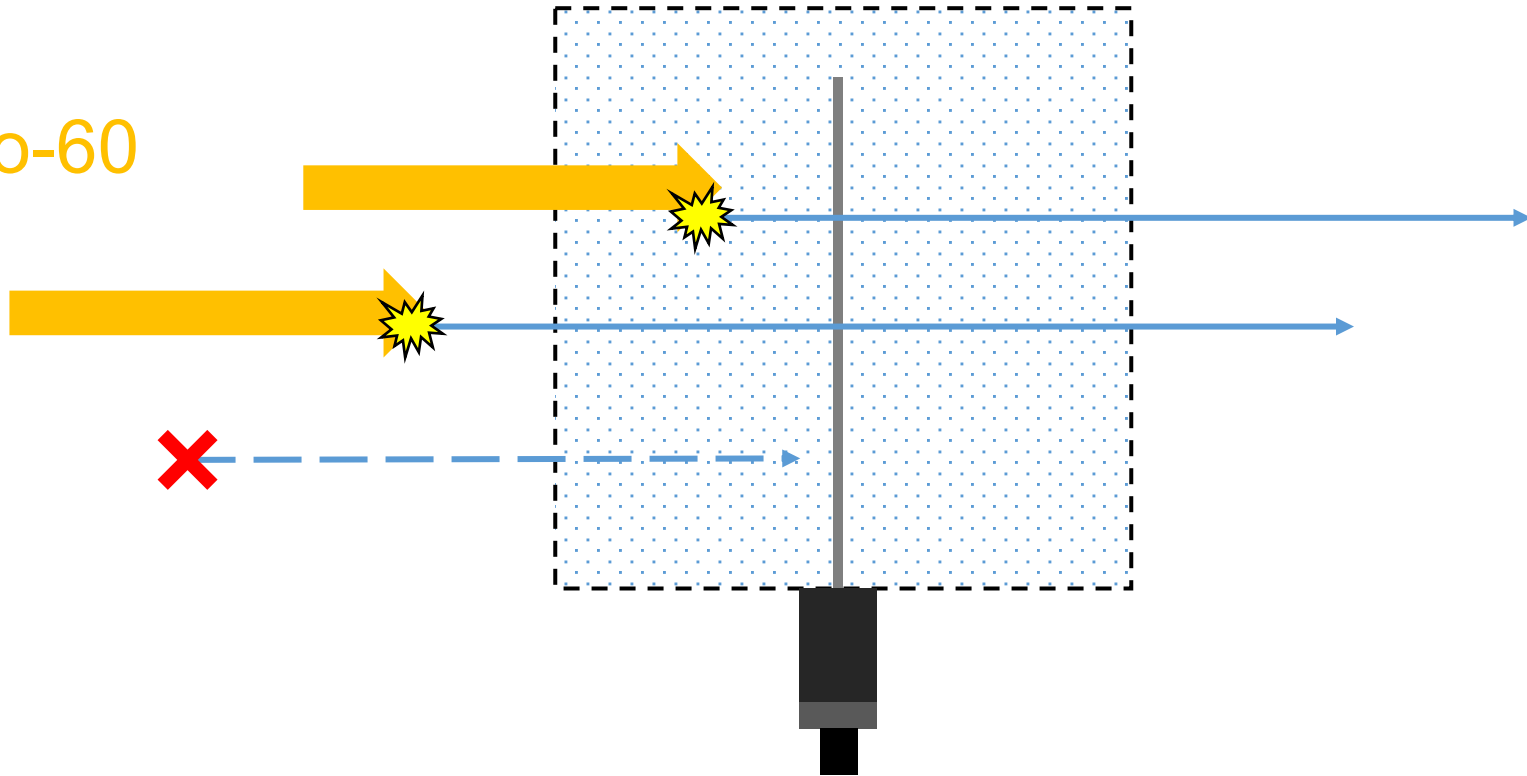
energy needed per ion pair

Measuring dose in free air

No CPE!

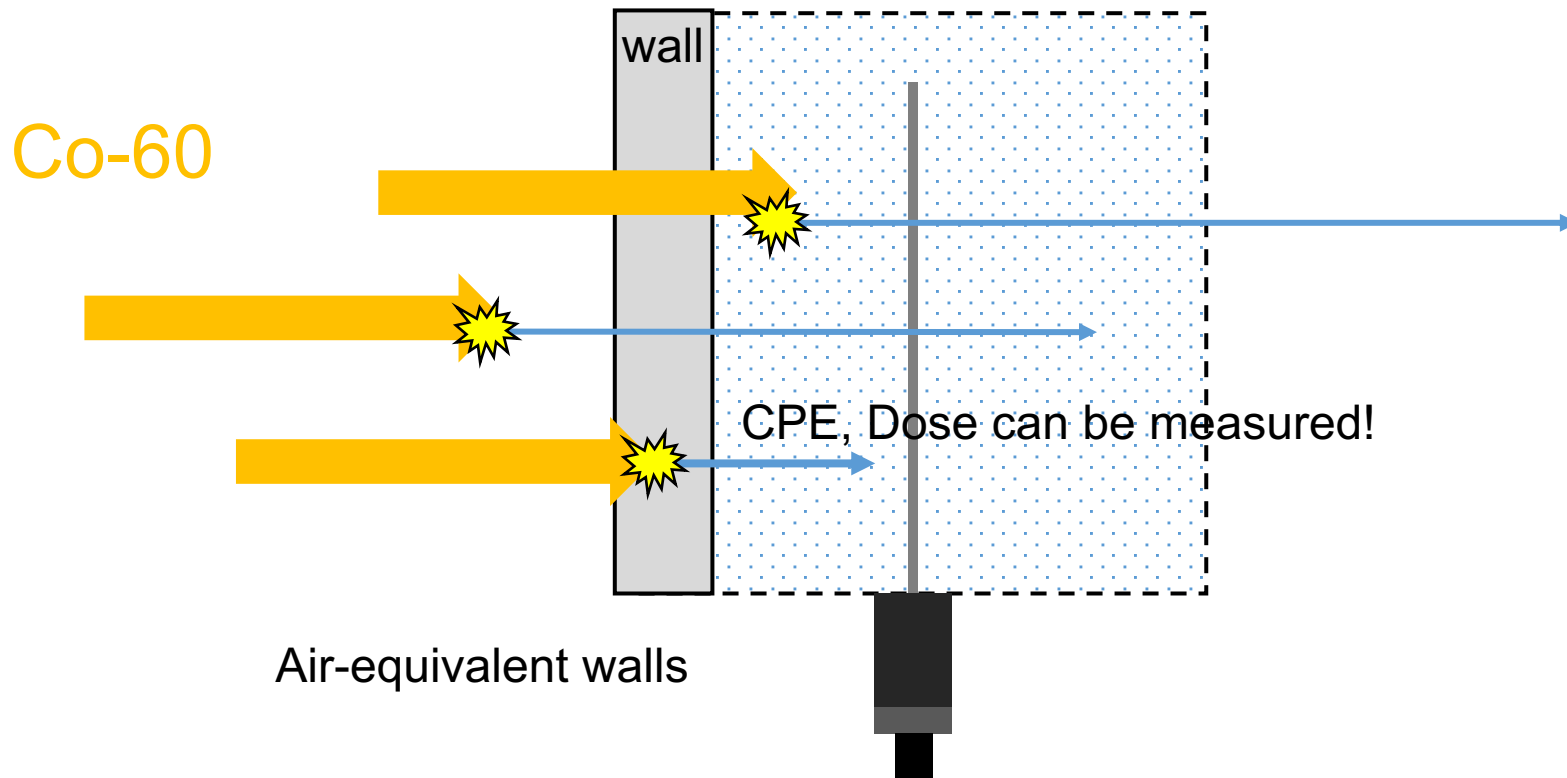
Dose cannot be measured!

Co-60

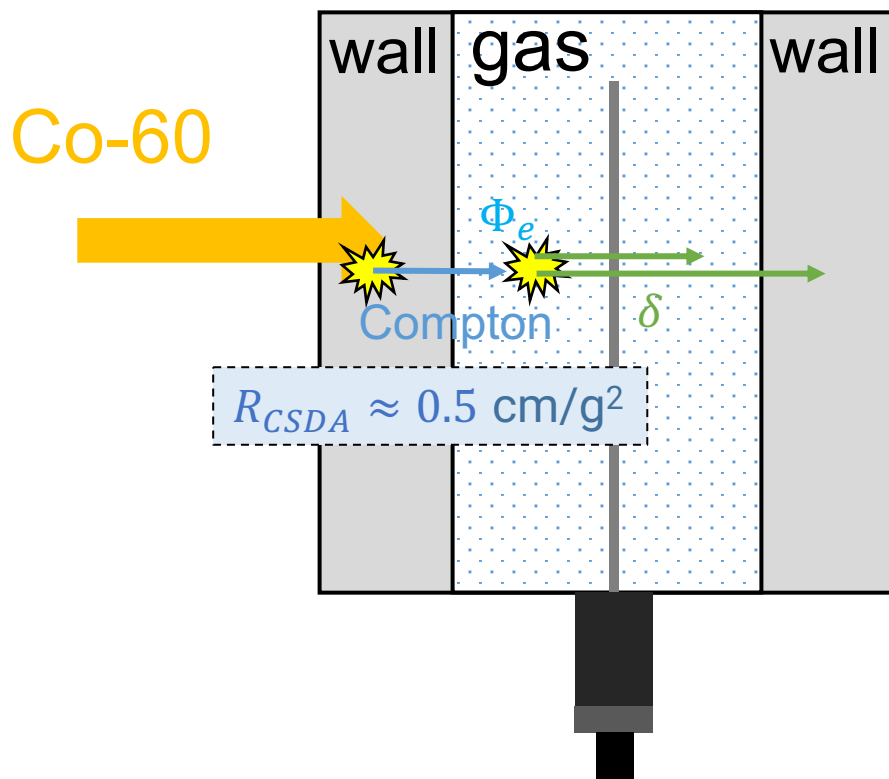


Free-air chamber (sagittal)

Measuring dose in free air



$$t' = 0.57 \text{ cm/g}^2$$



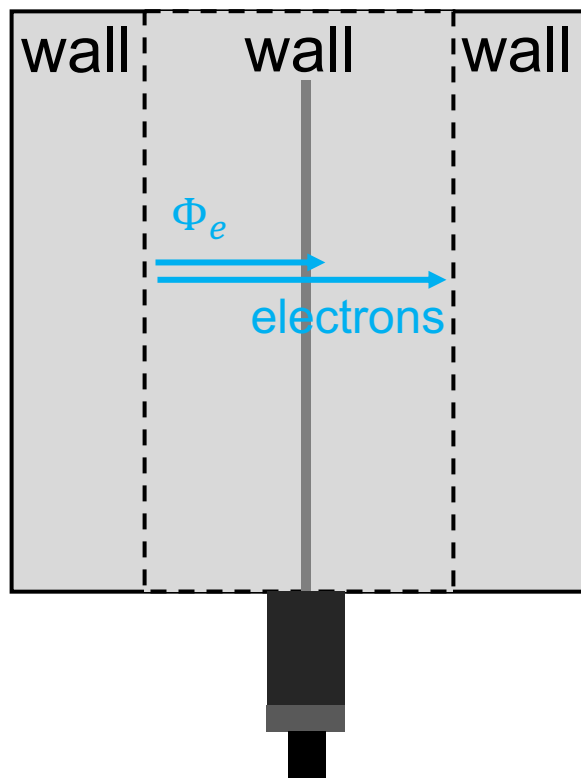
Ion chamber (sagittal)

Electron Perspective

$$D_{\text{gas}} = \Phi_e \left(\begin{array}{c} \bar{S} \\ - \\ \rho \end{array} \right)_{\text{gas}}$$

restricted by Δ

Electron Perspective

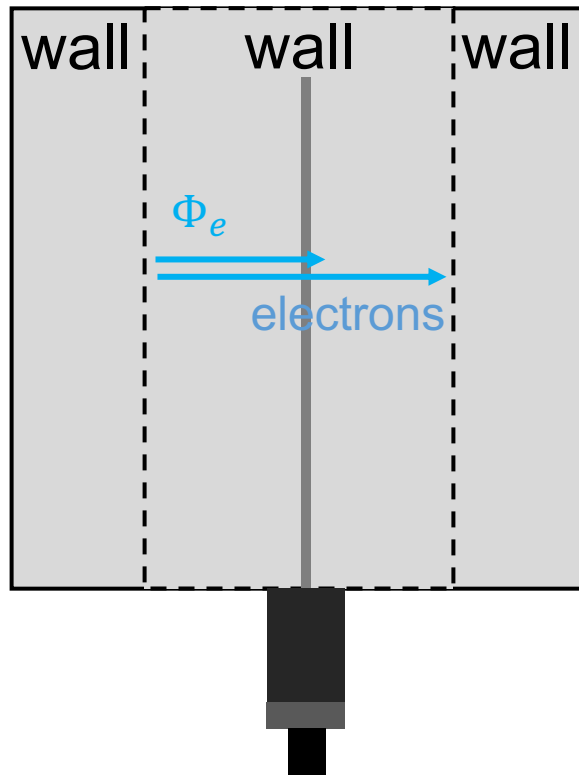


Ion chamber (sagittal)

$$D_{\text{wall}} = \Phi_e \left(\frac{\bar{S}}{\rho} \right)_{\text{wall}}$$

restricted by Δ

Electron Perspective



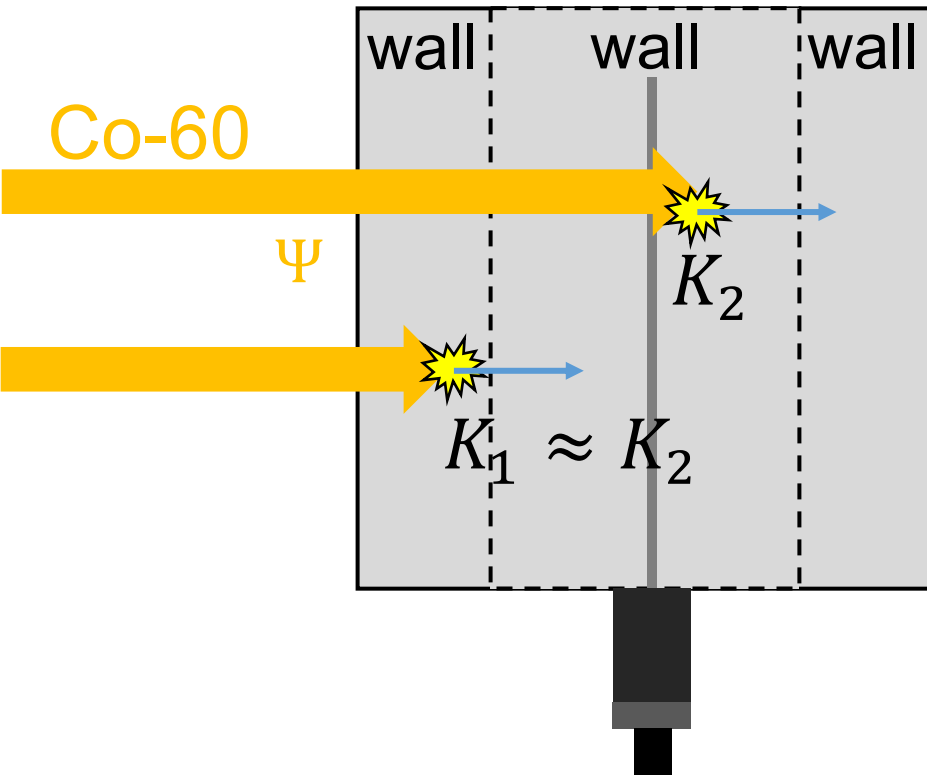
$$D_{\text{wall}} = D_{\text{gas}} \left(\frac{\bar{S}}{\rho} \right)_{\text{gas}}^{\text{wall}}$$

Ion chamber (sagittal)

Measuring dose via a chamber

Energy
Photon Perspective

Constant w/o attenuation



$$K_{c\text{wall}} = \Psi \left(\frac{\overline{\mu_{ab}}}{\rho} \right)_{\text{wall}}$$

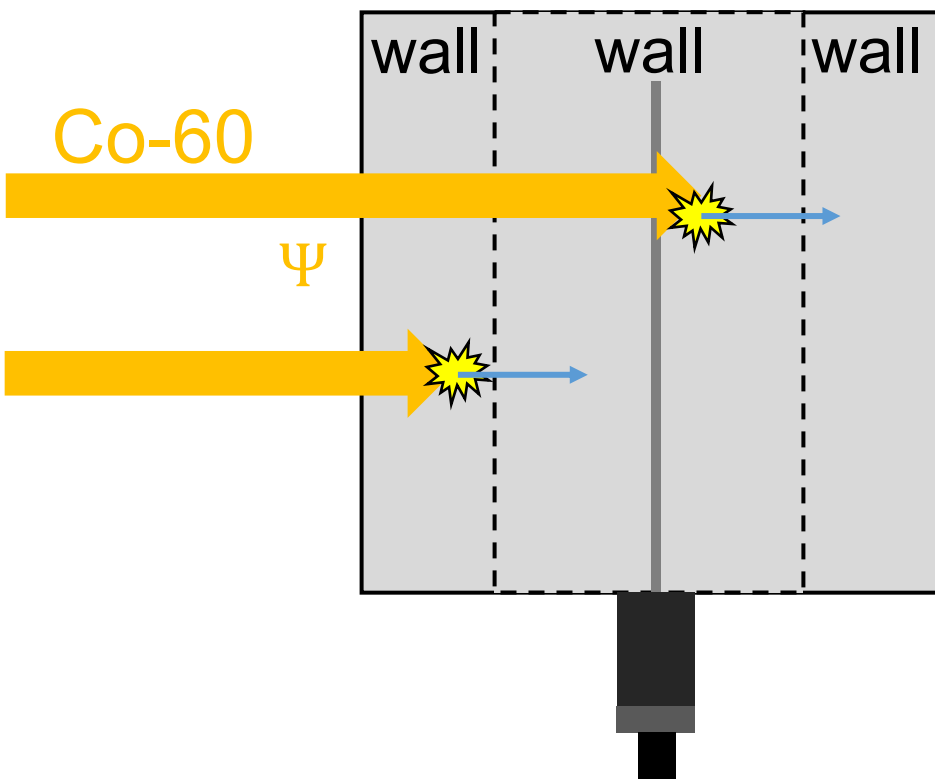
$$D_{\text{wall}} = B_{\bar{x}} K_{c\text{wall}}$$

Upstream Interaction

Ion chamber (sagittal)

Measuring dose in a chamber

Photon Perspective



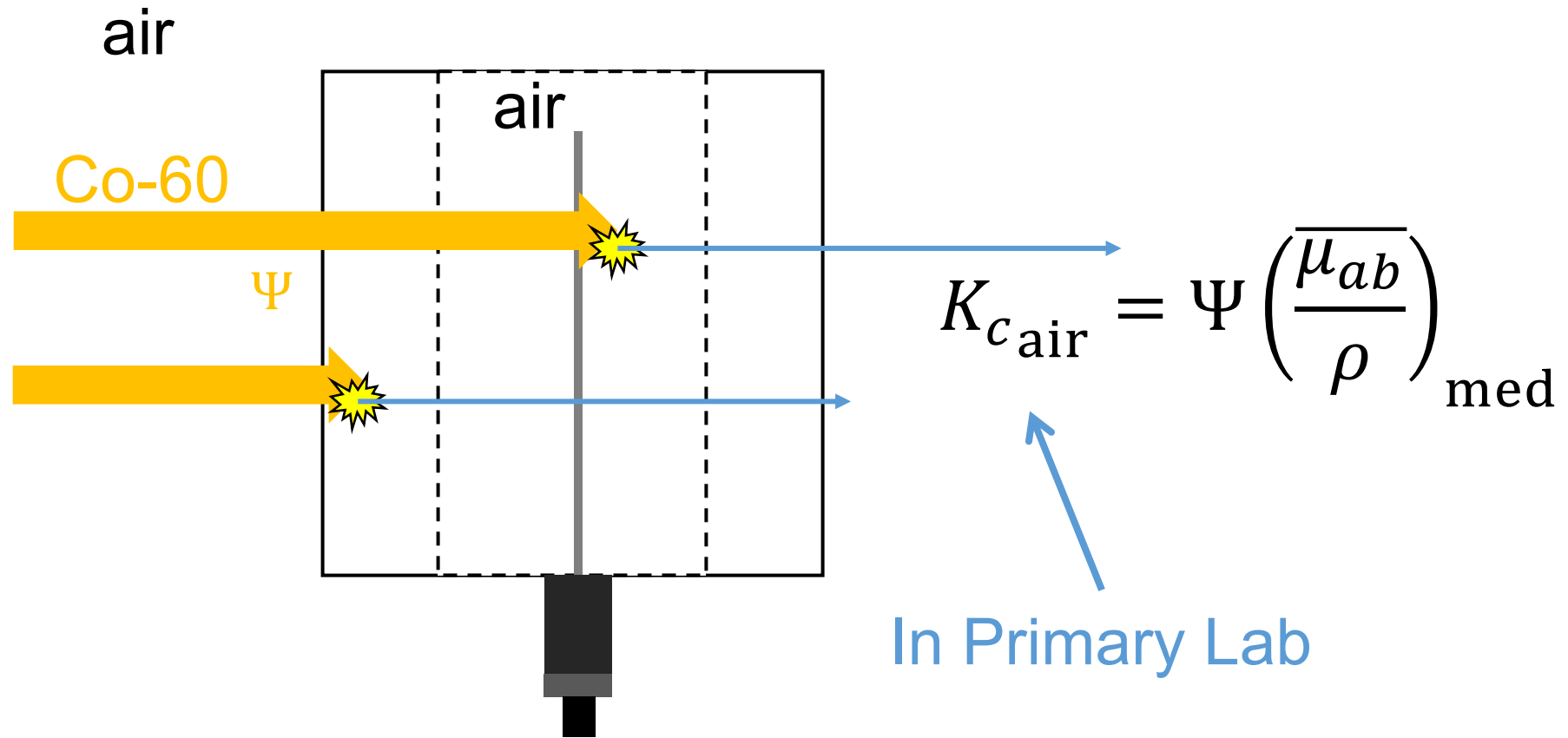
Ion chamber (sagittal)

$$K_{c_{\text{wall}}} = \Psi \left(\frac{\overline{\mu_{ab}}}{\rho} \right)_{\text{wall}}$$

$$D_{\text{wall}} = A_{\text{wall}} B_{\bar{x}} K_{c_{\text{wall}}}$$

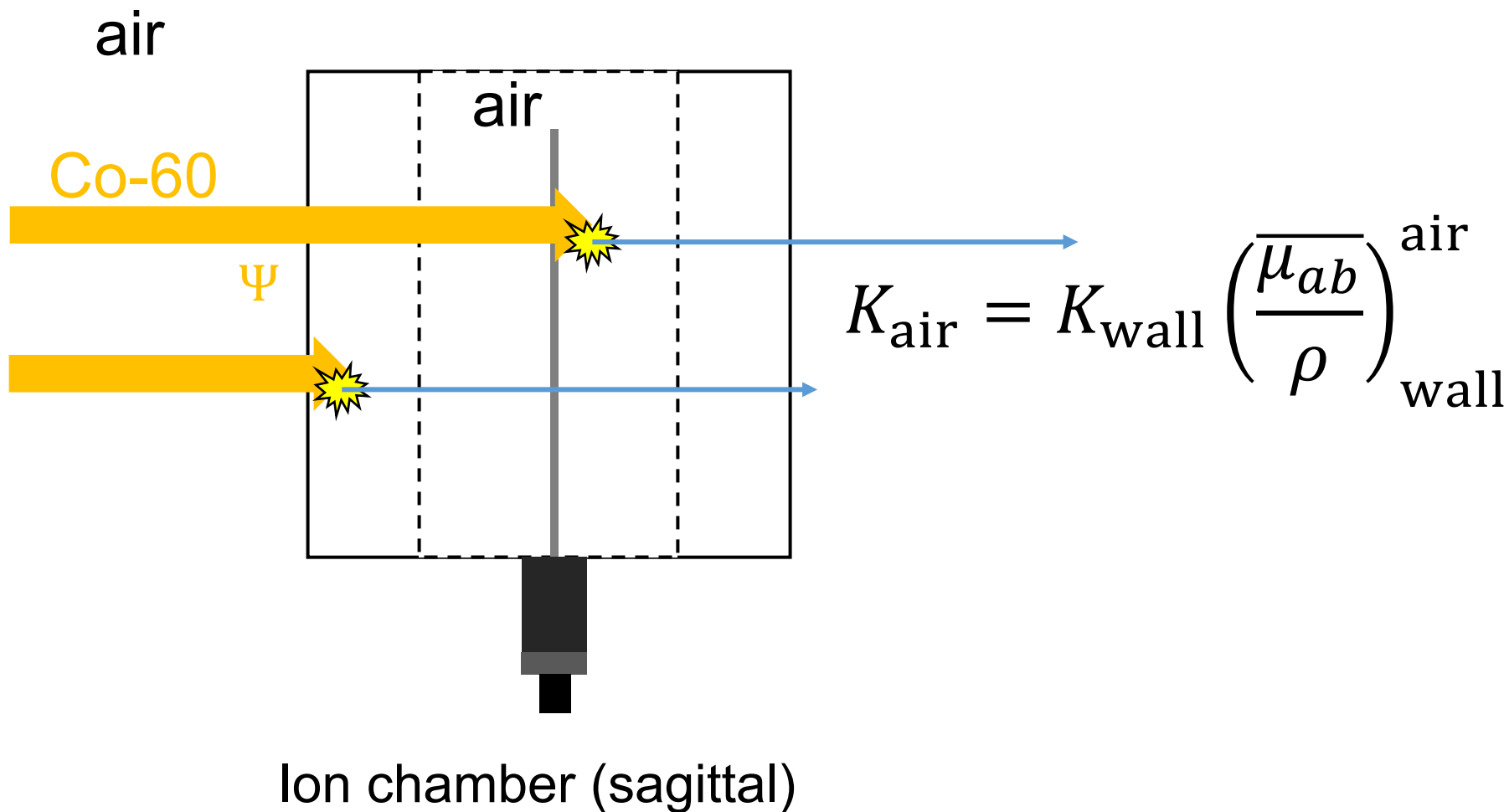
Attenuation

Measuring dose in a chamber

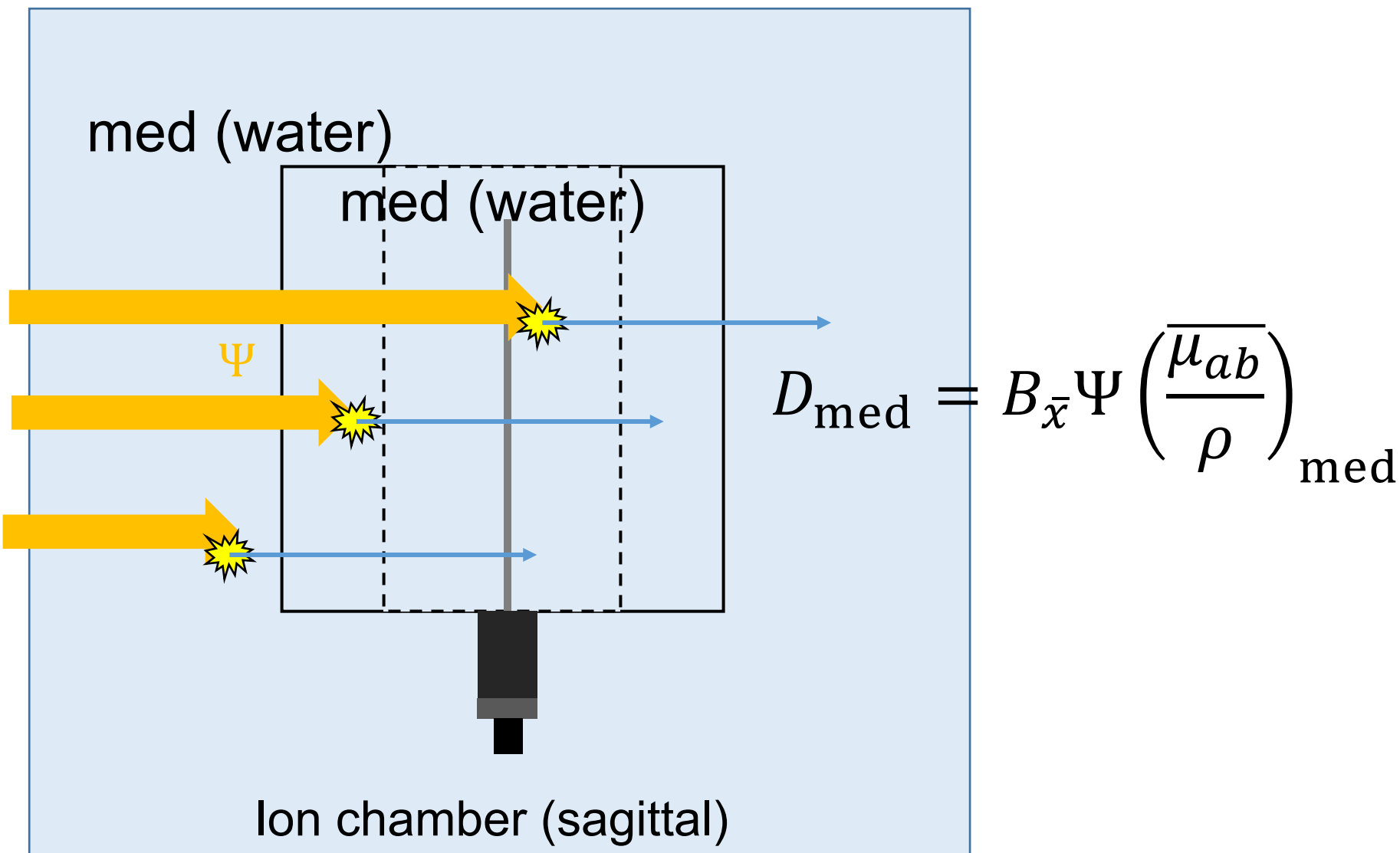


Ion chamber (sagittal) \approx free-air chamber

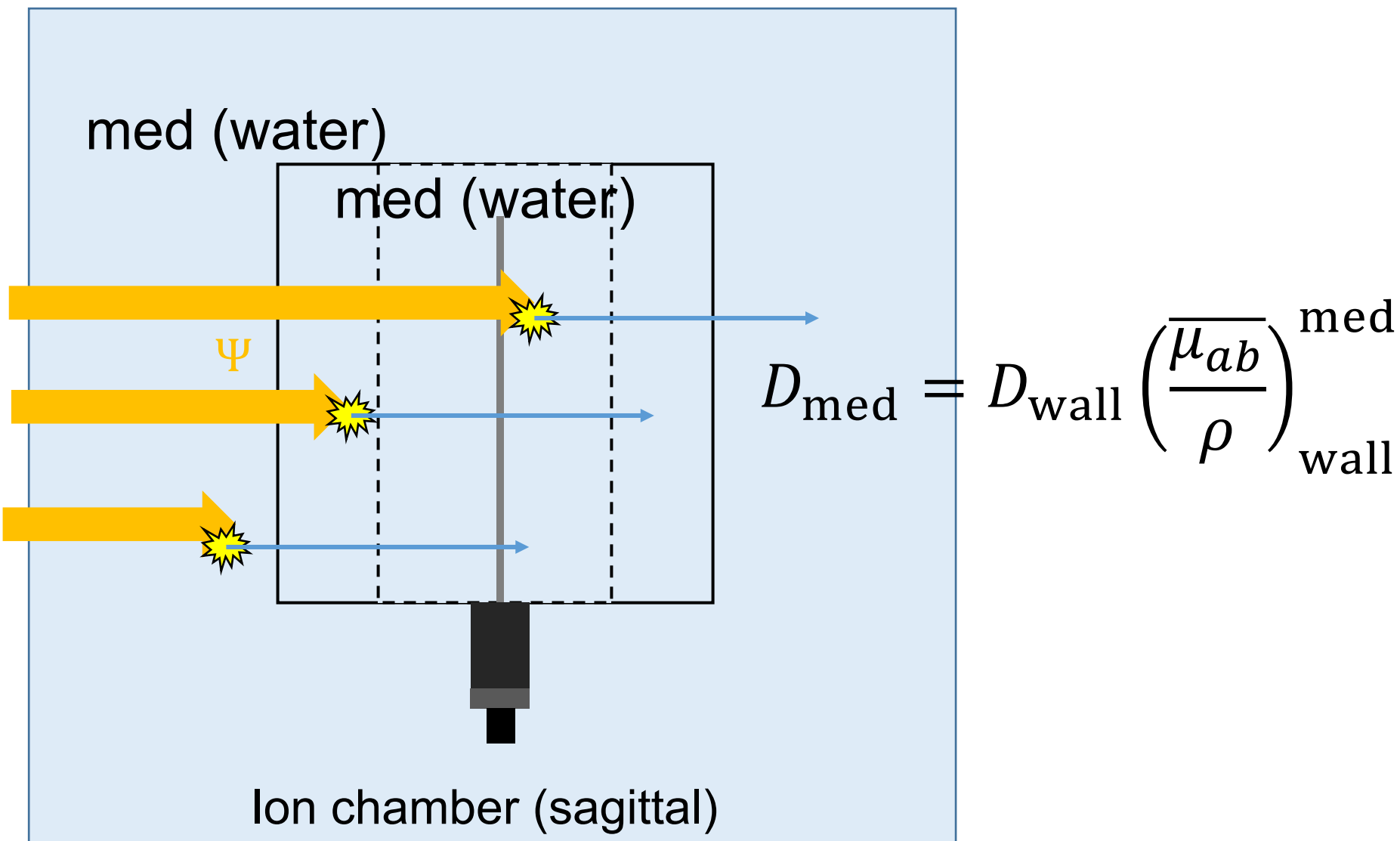
Measuring dose via a chamber



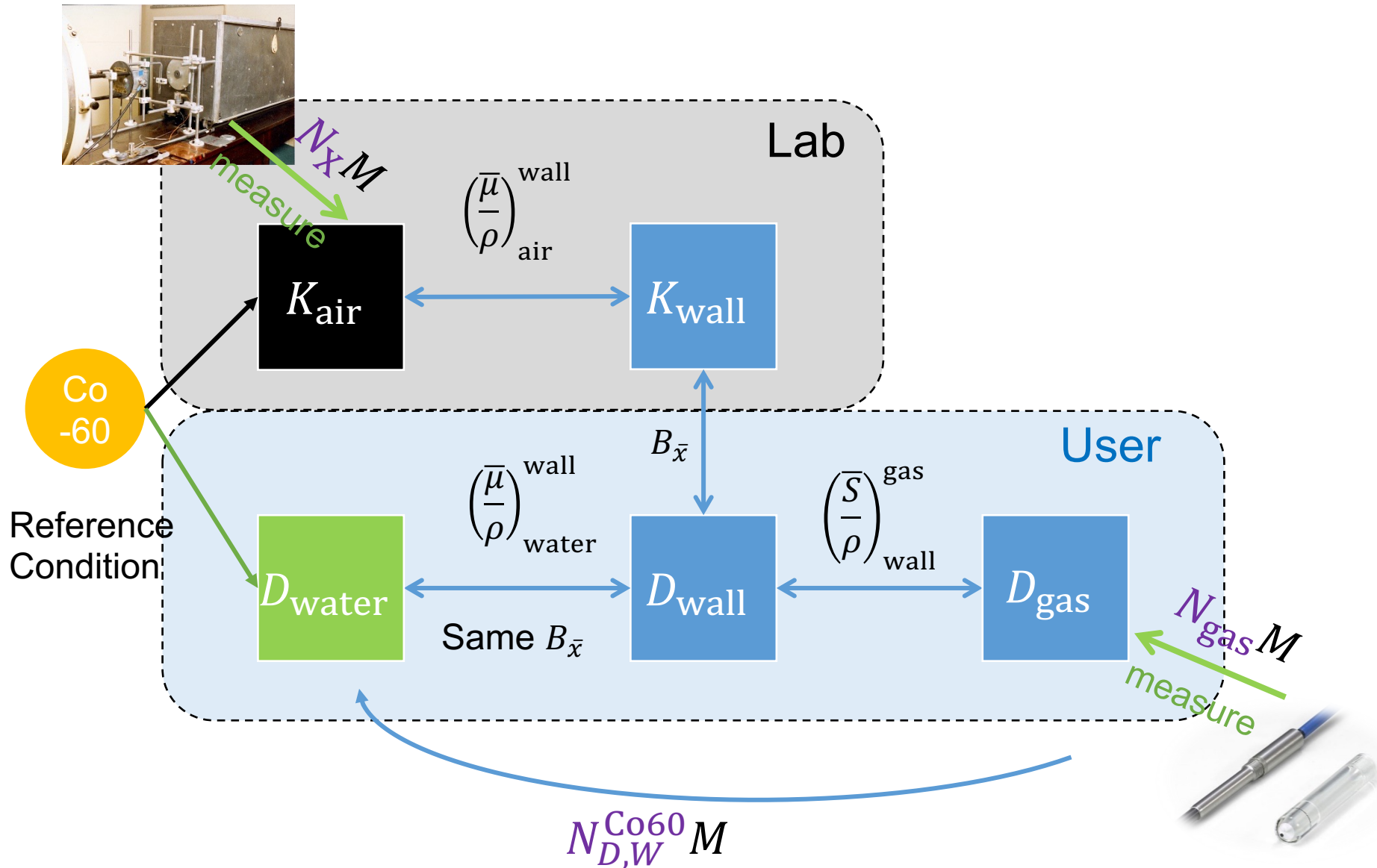
Measuring dose via a chamber



Measuring dose via a chamber



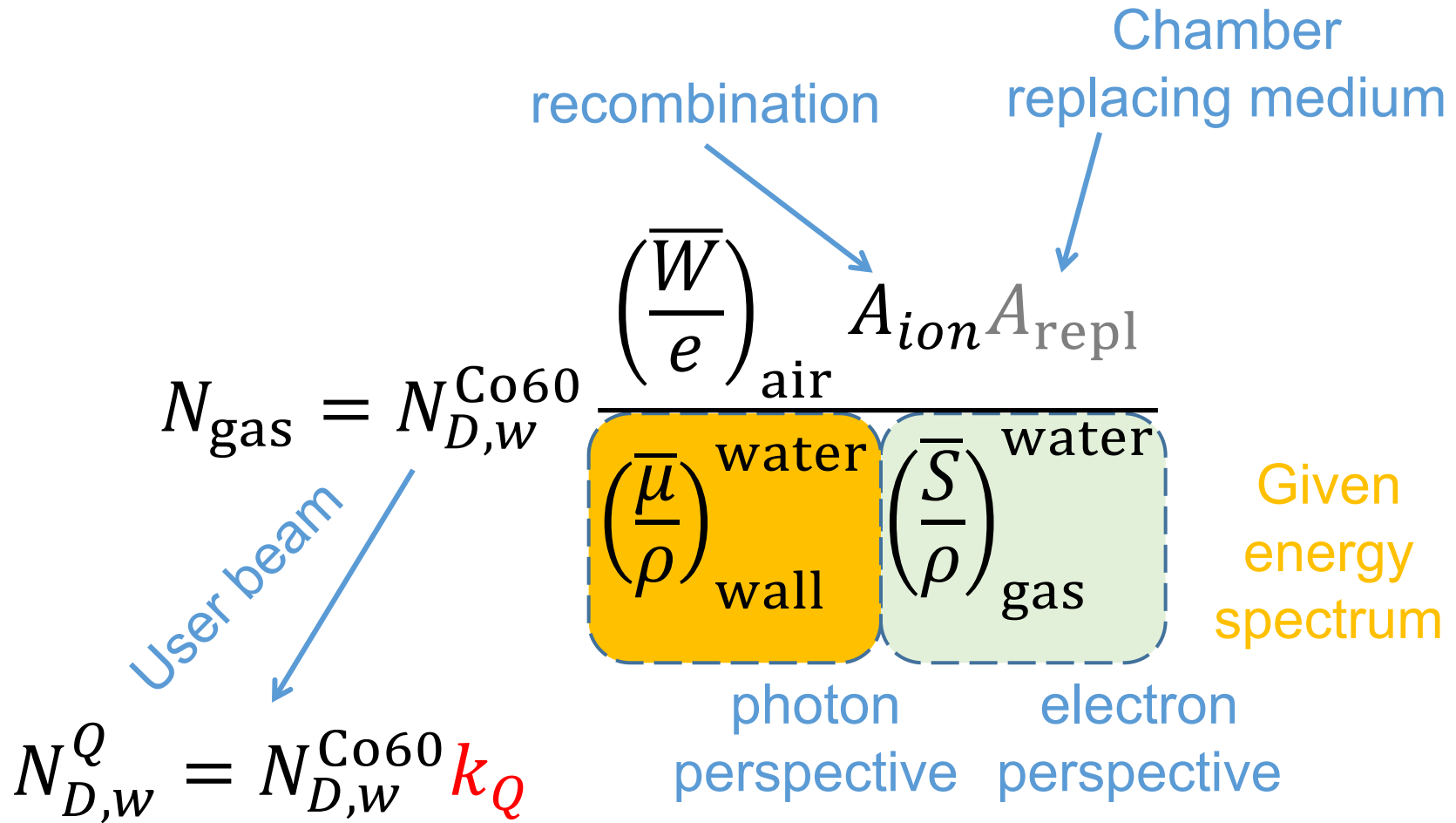
Summary of dose measurement



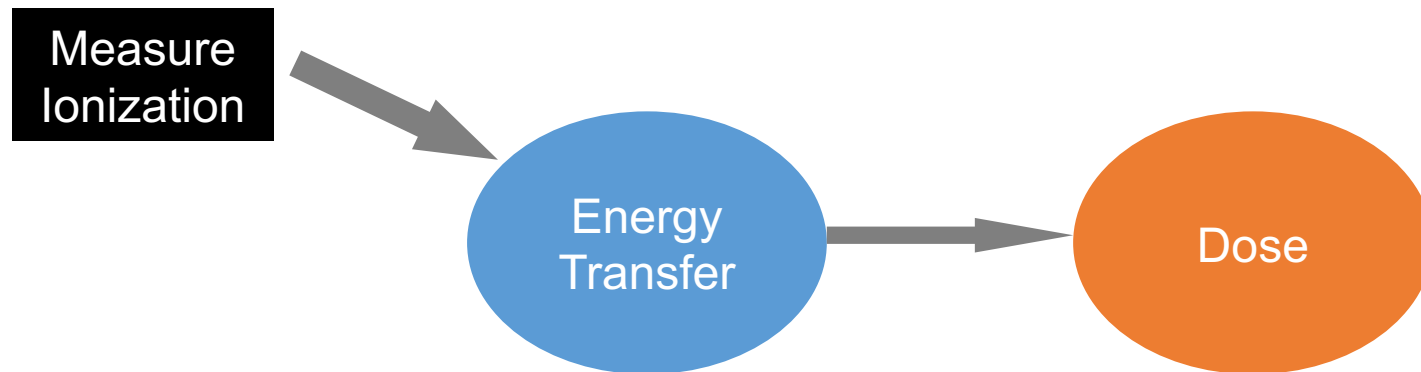
$$N_{\text{gas}} = N_X \frac{\left(\frac{\bar{W}}{e}\right)_{\text{air}} A_{\text{ion}} A_{\text{wall}} B_{\text{wall}}}{\left(\frac{\bar{\mu}}{\rho}\right)_{\text{air}} \left(\frac{\bar{S}}{\rho}\right)_{\text{wall}}}$$

recombination
attenuation
build-up

photon perspective
electron perspective



- We demystified TG-21 by understanding the process of energy transfer among radiation and charged particles and the process of dose deposition.
- We utilized cavity theory to measure dose through an ion chamber in the real world.



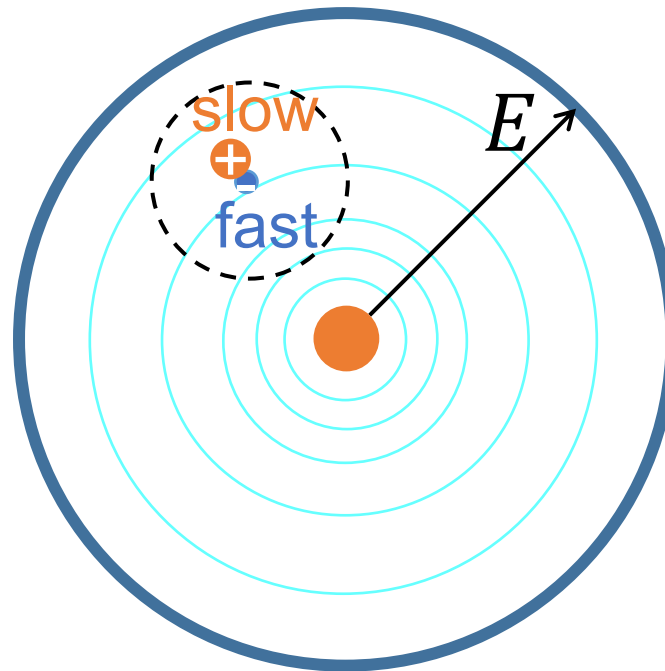


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University Hospital | **HEALTH**

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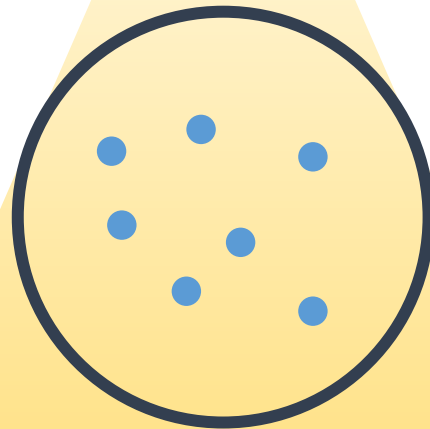
Rotation Mentor: Xiao Wang

Cylindrical chamber: what's good?



What is P_{TP} ?

Thinner air molecules,
Less chance of ionization!



Ion Chamber

Density of Quantity

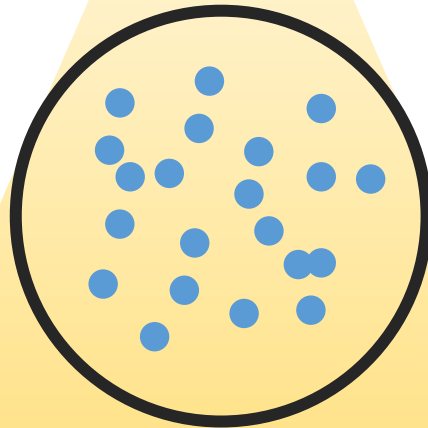
$$I \propto \rho = \frac{N}{V}$$

$$\propto \frac{nN_A}{V} \propto n$$

The amount of substance

What is P_{TP} ?

Denser air molecules,
More chance of ionization!

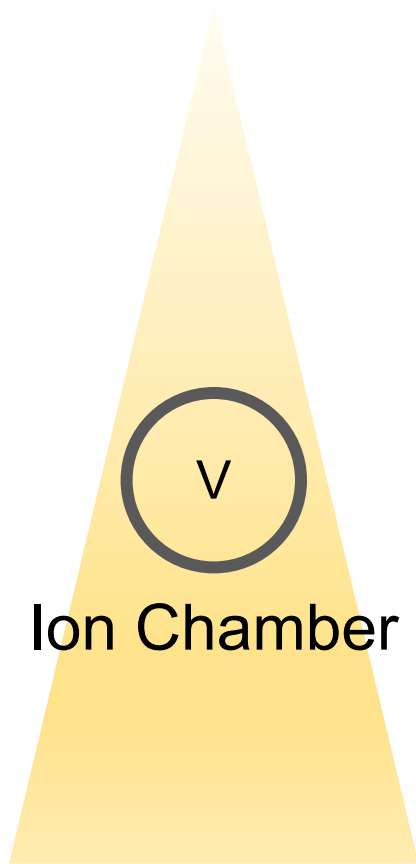


Ion Chamber

$$I \propto n$$

What is P_{TP} ?

- Ideal gas equation



$$PV = nRT$$

$$n \propto \frac{P}{T} \propto I$$

Air Density

Ionization

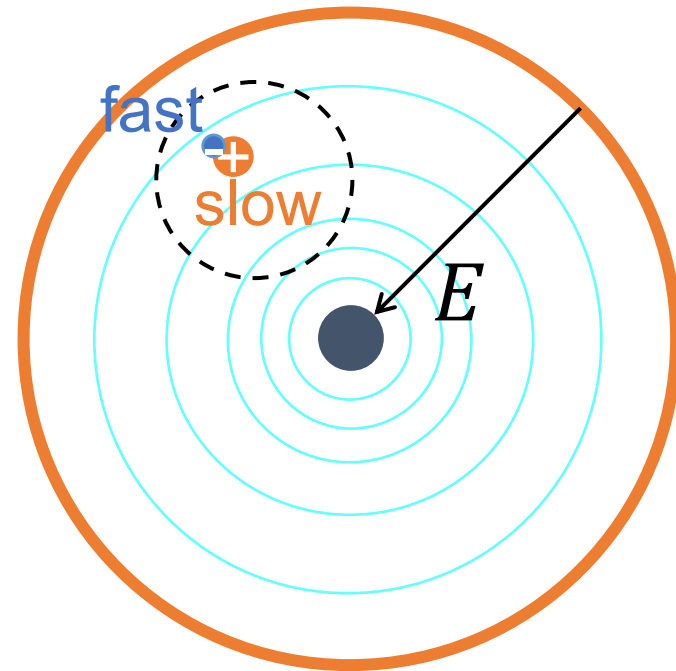
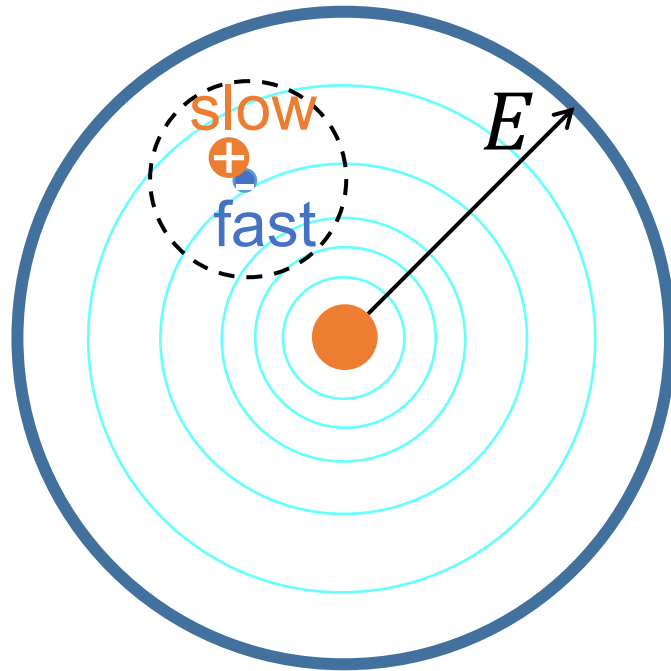
What is P_{pol} (polarity effect)?

$$P_{ion} = \frac{M_+ - M_-}{2M_+}$$

The diagram illustrates the derivation of the ionization polarization formula. It shows the equation $P_{ion} = \frac{M_+ - M_-}{2M_+}$. Above the equation, the terms $+300 \text{ V}$ and -300 V are written in yellow. Two yellow arrows point from $+300 \text{ V}$ to M_+ and from -300 V to M_- in the numerator of the fraction.

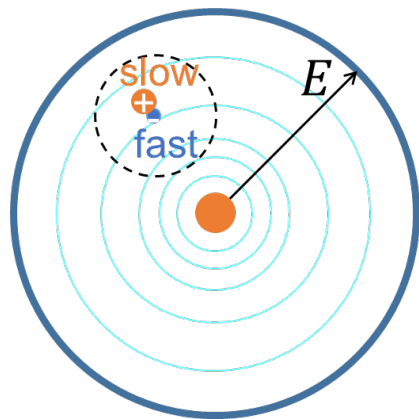
What is P_{pol} (polarity effect)?

- For a cylindrical chamber

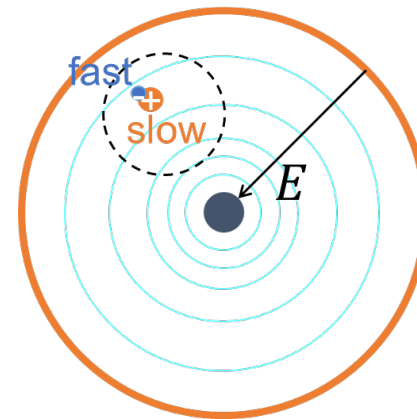


Recombination \uparrow
charge collection time \uparrow
(dead time \uparrow)

- We are supposed to collect 100 nC.



98 nC



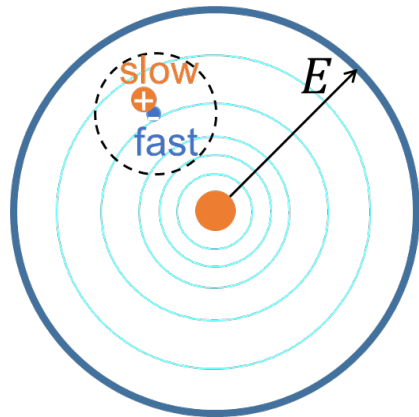
-95 nC

$$M_{corr} = M_{raw} \left(\frac{M_+ - M_-}{2M_+} \right) = 98 \times \frac{98 + 95}{2 \times 98} = 98 \times 0.985$$

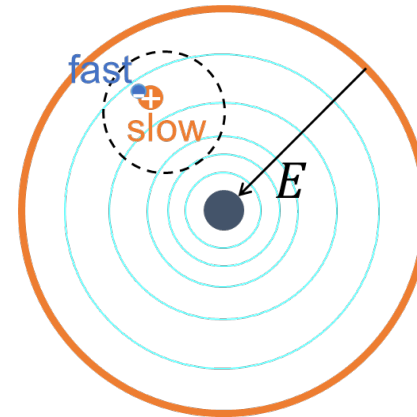
= 96.5 nC, even worse!!

Cause (I): the design

- We are supposed to collect 100 nC.



98 nC



-95 nC

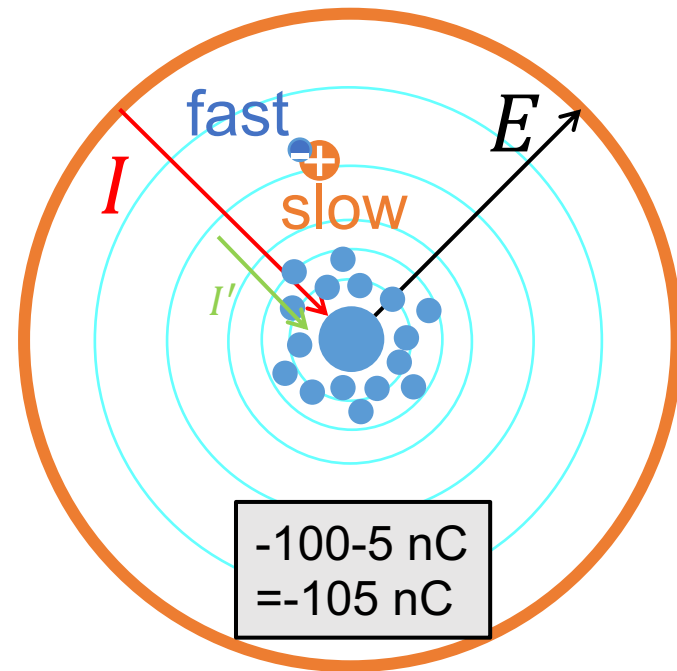
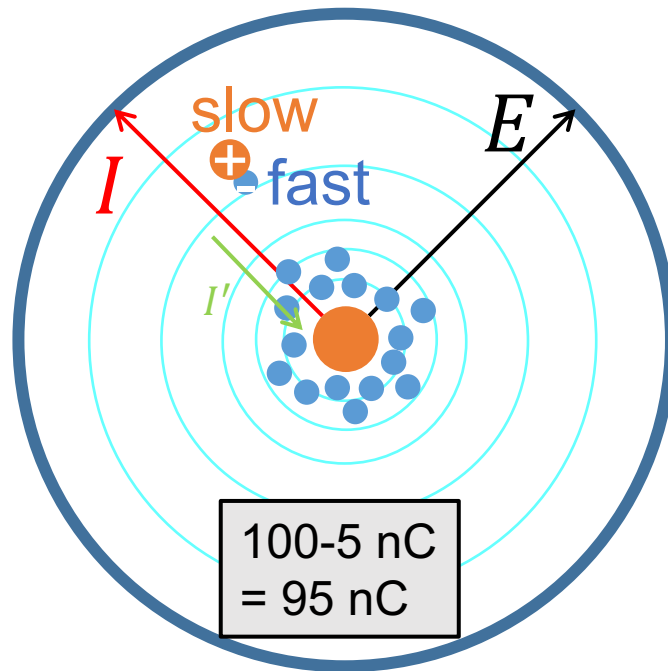
$$M_{corr} = M_{raw} \left(\frac{M_+ - M_-}{2M_+} \right) = 98 \times \frac{98 + 95}{2 \times 98} = 98 \times 0.985$$

= 96.5 nC, even worse!!

- TG-51 is not trying to correct polarity effect related to the chamber design.

Cause (II): Electron Contamination RUTGERS

- We are supposed to collect 100 nC.



$$M_{corr} = M_{raw} \left(\frac{M_+ - M_-}{2M_+} \right) = 95 \times \frac{95 + 105}{2 \times 95}$$

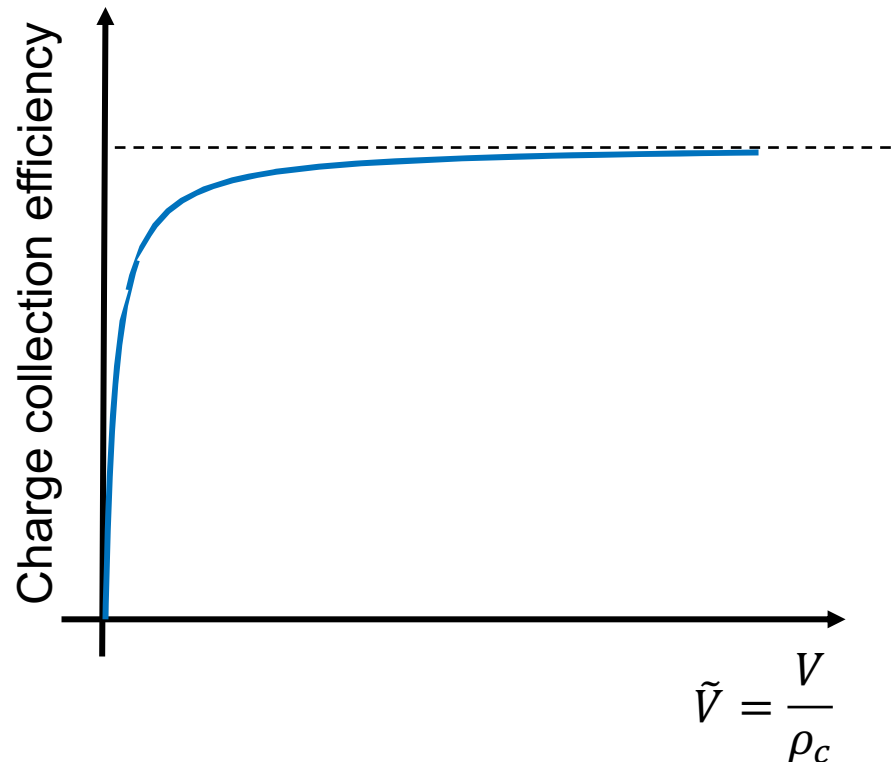
= 100 nC, perfect!!

Cause (II): Electron Contamination **RUTGERS**

- TG-51 corrects polarity effect related to any type of electric current contamination of a fixed direction.

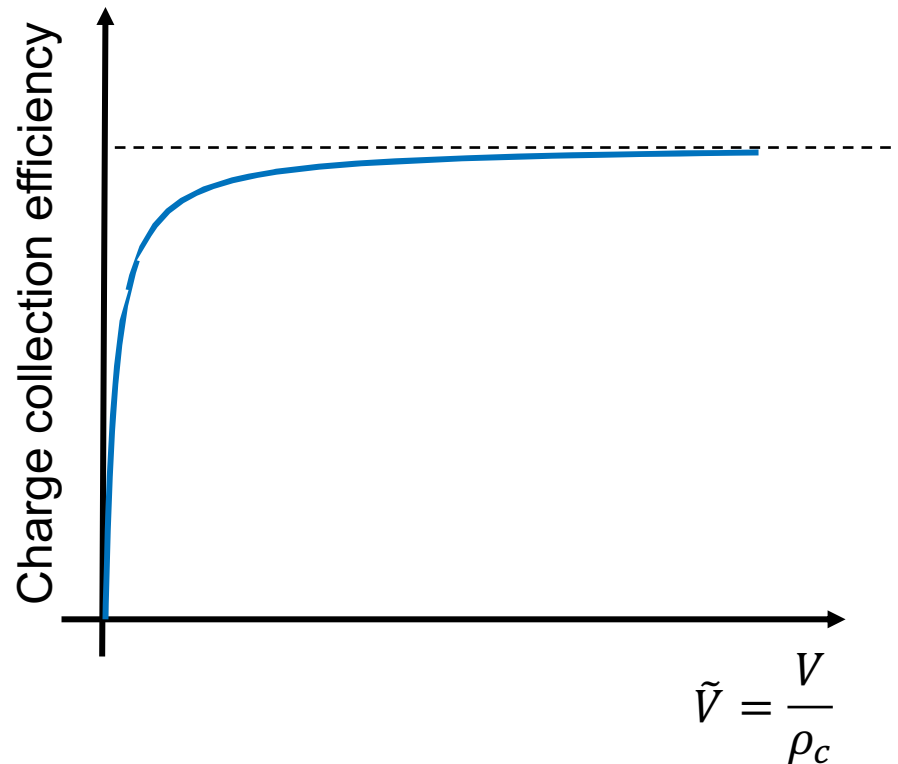
What is P_{ion} (recombination)?

- In principle, how to correct P_{ion} ?
 - Measure the collected charge at each voltage and then extrapolate to the limit.



What is P_{ion} (recombination)?

- In principle, how to correct P_{ion} ?
 - Measure the collected charge at each voltage and then extrapolate to the limit.

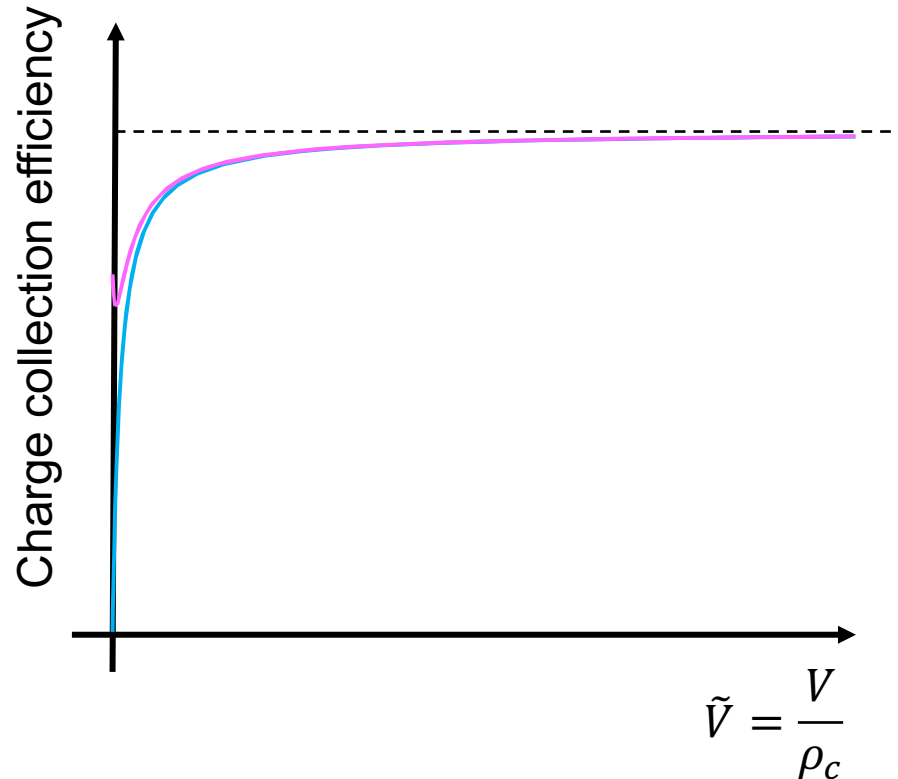


Theoretical model of P_{ion} .

$$p = \tilde{V} \ln \left(1 + \frac{1}{1 + \tilde{V}} \right) \quad p = \tilde{V} \left(\frac{1}{1 + \tilde{V}} \right) + \frac{3}{4} \left(\frac{1}{1 + \tilde{V}} \right)^2 + \dots$$

Pulsed Beam

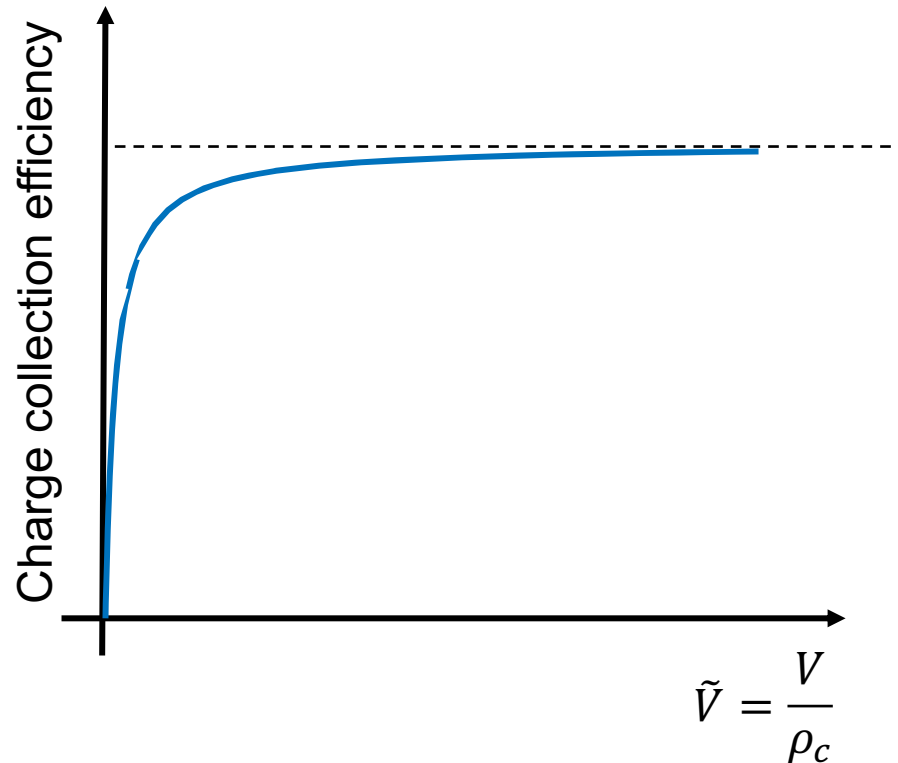
Pulsed-swept Beam



Theoretical model of P_{ion} .

$$p = \frac{\tilde{V}}{1 + \tilde{V}}$$

Charge collection efficiency



- Charge collection efficiency:

$$p = \frac{\tilde{V}(\rho)}{1 + \tilde{V}(\rho)}$$

- The so-called “two-voltage” technique:

$$M_H = Cp_H = \frac{\tilde{V}_H(\rho)}{1 + \tilde{V}_H(\rho)} \quad M_L = Cp_L = \frac{\tilde{V}_L(\rho)}{1 + \tilde{V}_L(\rho)}$$

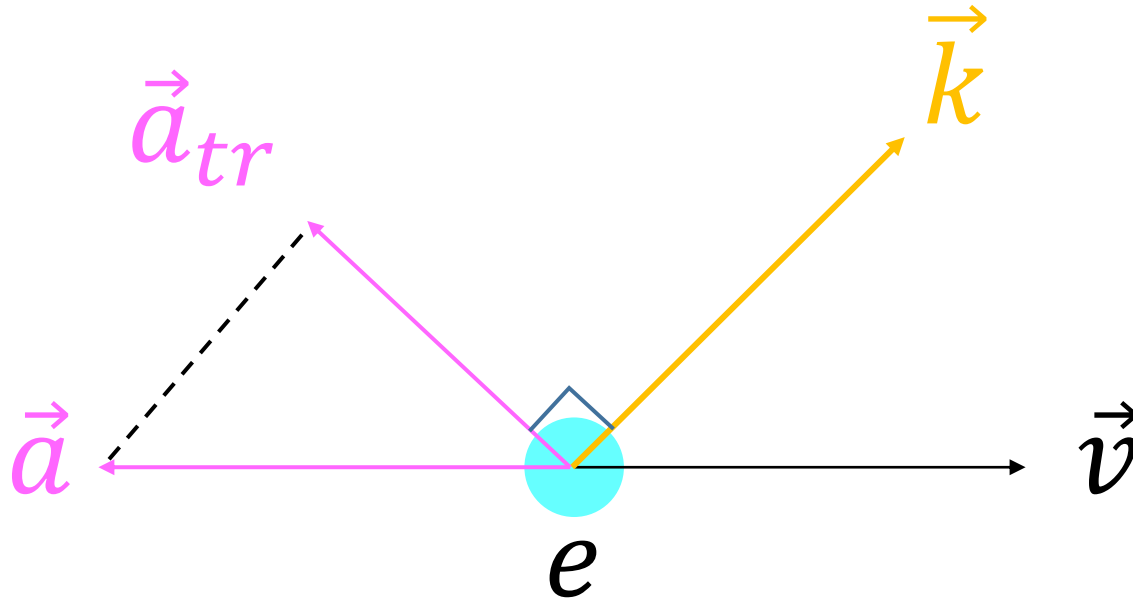
Solve for p_H

How TG-51 correct P_{ion} .

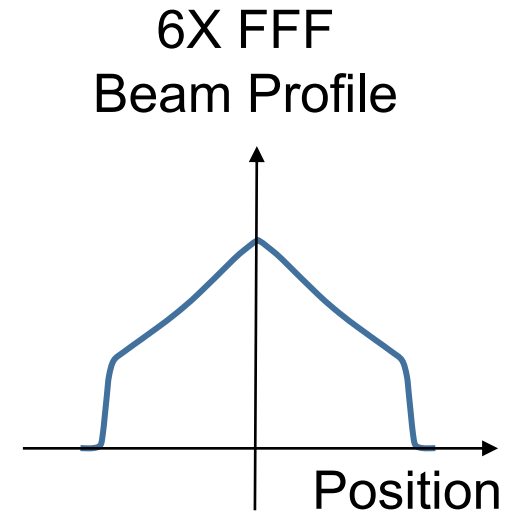
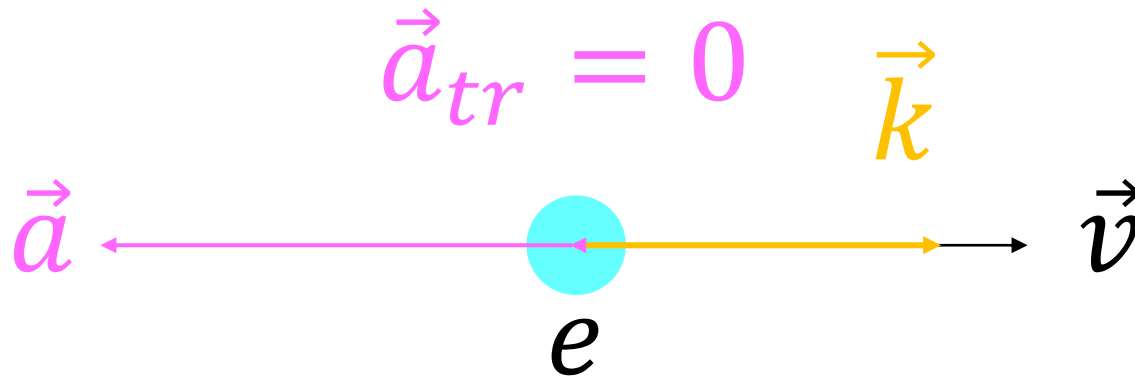
$$p_H = \frac{1 - \frac{V_H}{V_L}}{\frac{M_H}{M_L} - \frac{V_H}{V_L}}$$

Solve for p_H

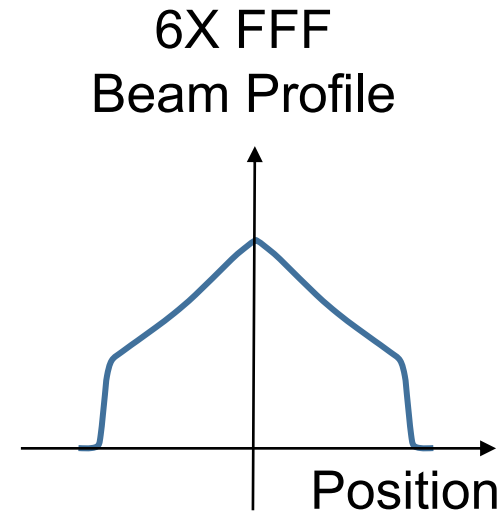
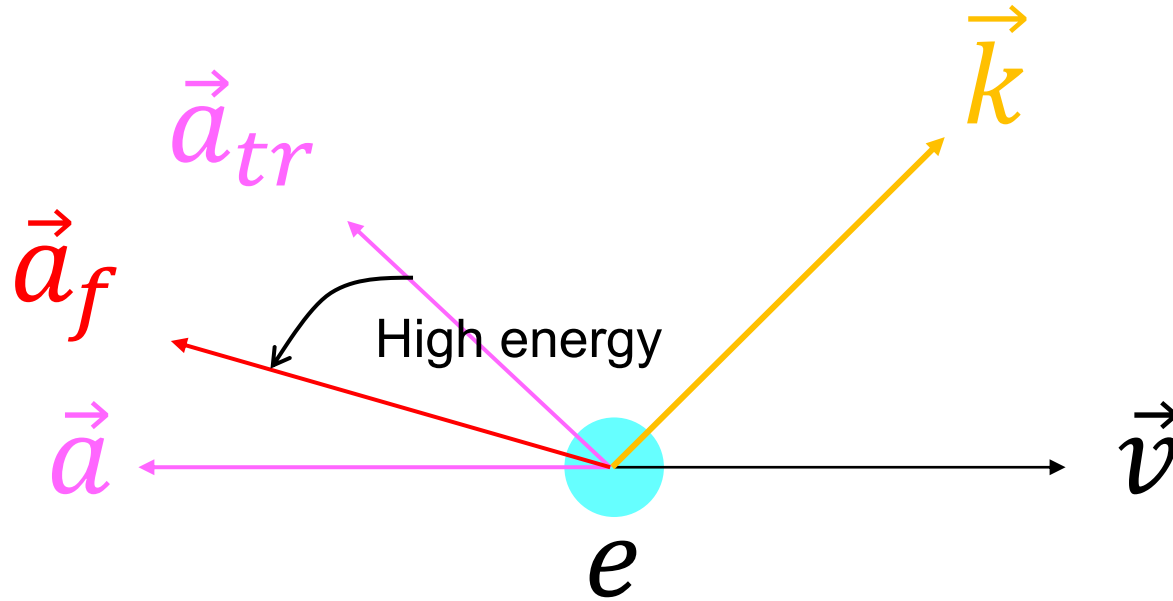
The physical picture of radiation stopping power



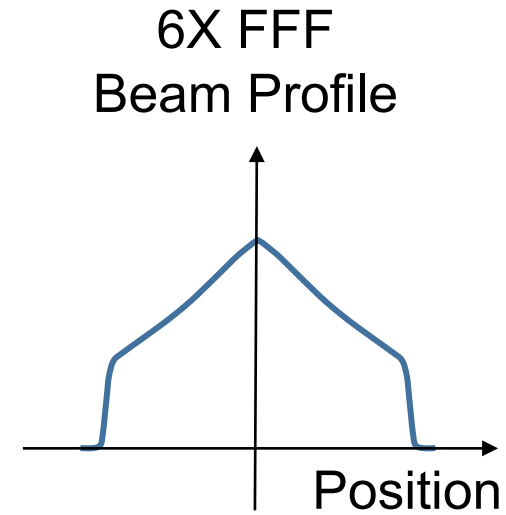
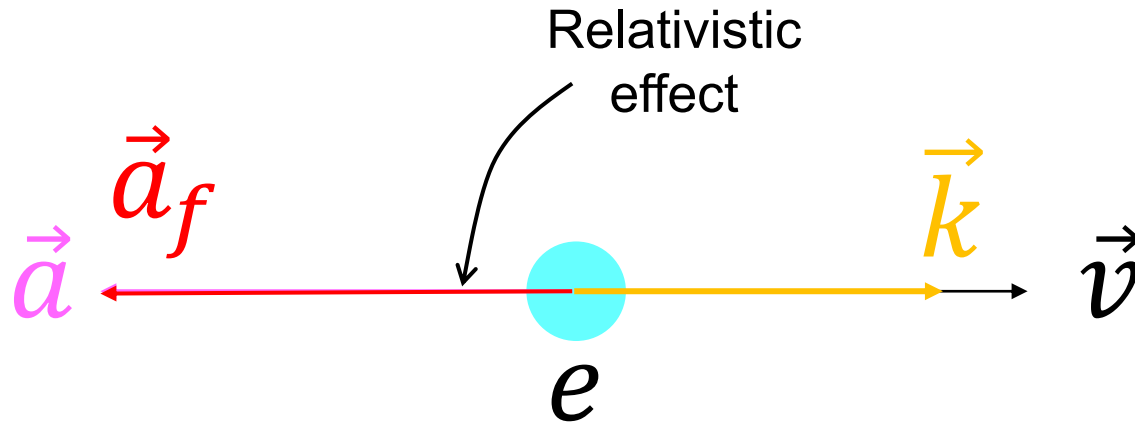
The physical picture of radiation stopping power



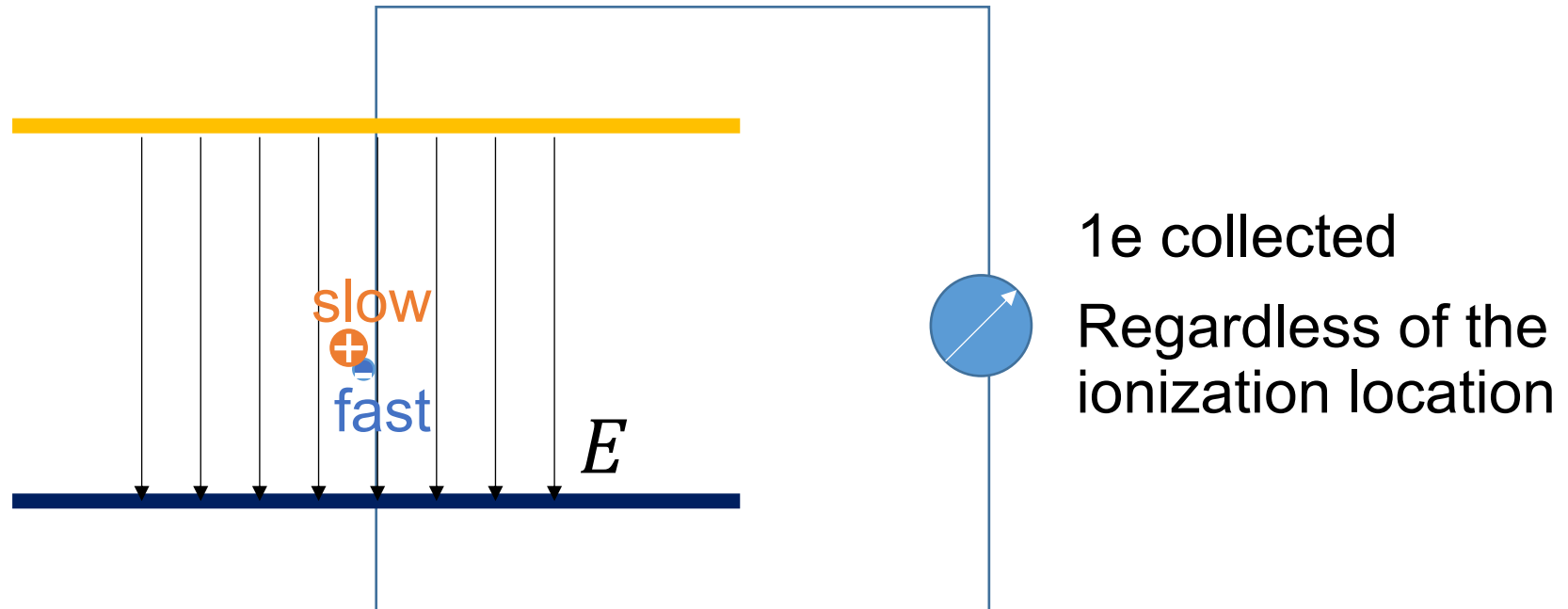
The physical picture of radiation stopping power



The physical picture of radiation stopping power



Electrometer reading corrections



$$M = M_{\text{raw}} P_{\text{ion}} P_{\text{pol}} P_{\text{TP}}$$